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Petri net-based methods for analyzing structural security in e-commerce business processes

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HIGHLIGHTS

- A framework for analyzing structural security in e-commerce business process.
- A method of modeling control and data structures for constructing an e-commerce business process.
- Petri net-based modeling and analysis methods.

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ABSTRACT

The rapid development of e-commerce worldwide, means more e-commerce business processes adopting the structure of multiple participants; these include shopper clients, merchant and third-party payment platforms (TPPs), banks, and so on. It is a distributed and complex system, where communications among these participants rely on the web services and Application Programming Interfaces (APIs) such as Cashier-as-a-Service or CaaS. This introduces new security challenges due to complex interactions among multiple participants, and any design flaws in procedure structures may result in serious security issues. We study the structural security issues based on Petri nets, and a framework for analyzing structural security in e-commerce business process is proposed. Petri net-based modeling and analysis methods are also provided. Given the specifications of e-commerce business processes, the proposed methods can help designers analyze structural security issues of an e-commerce business process.

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1. Introduction

E-commerce has significantly developed in recent years, and more and more business is conducted over the Internet. The daily volume of e-commerce is sizable and continues to grow at a rapid pace. Many e-commerce platforms spring up to accelerate this new industry [1,2]. E-commerce systems with multiple participants, including third-party payment platforms (TPPs), e-commerce systems, banks, clients, and other applications, have become the new frontier for conducting business. As a distributed application on the web, e-commerce business processes are more complex and loosely coupled. The participants communicate with each other through web services and APIs such as Cashier-as-a-Service or CaaS [3,4]. The business processes of different participants construct the entire process structure. This integration introduces new

security challenges due to complex interactions among the APIs of multiple interactive participants. These differ from traditional security issues, and the new security challenges do not refer to virus, Trojans or security protocols [5,6]. The complex structural linkage of control and data flows in e-commerce systems may produce very serious problems including the violation of the transaction properties, and losses of user funds. These issues can be defined as structural security. There are many structural security cases that have appeared over recent years. These include the vulnerability caused by a combination of open source online shopping system and TPP [3], “one yuan gate” event of Taobao in 2011 [7], and mongodb-based web applications [8].

Business processes of e-commerce systems are the key, and it is difficult to correctly design the business structure. Modern businesses are inherently process-driven, and the security of business processes is increasingly important [9–12]. Most of the existing research around security business processes focuses on the security properties like Access Control and Confidential Information [9,10]

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in enterprise business processes. Other related studies refer to the process consistency in complex business processes [11,12]. These works are proposed to deal with the inconsistencies among business processes of different departments in a cross-organizational process. However, this research belongs to traditional security issues, and is insufficient to cope with structural security.

Petri nets are a suitable tool to illustrate true concurrency and model distributed systems, and Petri net-based approaches [13–16] have been presented to model and verify correctness and soundness of workflows. A series of works have been done on cooperative systems and inter-organizational workflow based on Petri nets [17–19], and other work has also been conducted on Petri net-based analysis and composition of web services [20–24]. These mainly focus on the soundness and correctness of workflow, cooperative systems, and composition of web services, but fail to consider structural security related to the financial security issues that are related to the funds of legal users.

In order to depict e-commerce business processes of multiple participants at both application-level and design-level and consider financial security issues, a formal model called an e-commerce Business Process Net (EBPN) is proposed [25,26]. Usage enables a designer to identify errors in the design process and correct them before the deployment phase. EBPNs are suitable for modeling and verifying e-commerce business processes, but their usage in structural security remains minimal. As part of our research, we use EBPN to model structural security issues in e-commerce business processes. First, we discuss the structural security, and propose a framework for analyzing methods. Then, Petri net-based modeling and analyzing methods are provided, including behavioral sequence and incidence matrix methods. Given the specifications of e-commerce business processes, the proposed methods can help designers analyze structural security issues of an e-commerce business process.

The remainder of this paper is organized as follows. Section 2 introduces the motivation example. Section 3 discusses the structural security issues. Section 4 presents the basic concepts. Section 5 describes how to model an e-commerce business process and structural properties using EBPN. Section 6 is the analyzing methods. Section 7 concludes this paper.

2. Motivation example

There is an actual e-commerce business process integrating Interspire and Google Checkout from [1]. For illustrating our method clearly, it is abridged, and we only focus on the most important functions; this is because it is a distributed and complex business process structure. The basic and important business process is shown in Fig. 1. Interspire utilizes several APIs to add/remove items in the shopping cart, which are aggregately denoted by API: Update Cart in the figure. The checkout process is triggered when the shopper clicks on the “Google Checkout” button. An important feature of this business process is that no order is generated before the payment is made: the shopper is supposed to pay for the content of his shopping cart first; only when the merchant is informed by the CaaS, the merchant will create an order of the transaction according to what is inside the cart and set its status to “PAID”, as illustrated in Table 1. The problem here is that this procedure is not atomic: after receiving the message of Step 4, the shopper does not send the message of Step 5 immediately. Instead, he can still call API: Update Cart to change or add new items to his cart. Then, when the message of Step 5 is sent, the current cart in the shopper’s session is more expensive than the cart field in Step 5. On the other hand, API Handle Payment loads the cart directly from the shopper’s session, rather than from the CaaS, to build the order. This causes an inconsistency between what the CaaS sees in the cart at the paid time and what the merchant has at the checkout

Table 1

Key functionalities of the business process in Fig. 1.

TStore.com/handleIPN:
1: if (GetMsgField(“status”) ≠ PAID) exit; /*payment status*/
2: cart = LoadShoppingCart(GetMessageField(“sessionID”));
3: order = CreateOrder(cart);
4: order.status = PAID;

completion time, so the shopper can pay for a cheap item, but check out many expensive items [1].

This is a typical case of structural security. The structure of business process is the key, and integration of multiple participants introduces new security challenges due to complex interaction structures among Application Programming Interfaces (APIs). The wrong design of business structures would result in security accidents and the financial loss of legitimate users. Thus, one needs to exploit the methodologies to model and verify the structural security of online shopping business processes. Nevertheless, rigorous and formal methodologies for structural security issues remain largely open. The most pressing challenge is how to depict the business structure and structural security properties. In the following section, we discuss the related concepts of structural security.

3. Related concepts

Petri nets are a graphical language for modeling and validating concurrent and distributed systems, and allow true concurrency instead of an interleaving-based semantics. Petri nets provide an explicit representation of both states and events and can be understood easily by a graphical representation of modeled systems. They have well-defined formal semantics and a wide range of formal analytical methods. The basic concepts of Petri nets are summarized in [27–29]. In order to describe the electronic trading process better, EBPN extends them with some new functions. The following definitions are from [25] and [26], and more details can be seen in the two references.

Definition 1 (EBPN). An E-commerce Business Process Net (EBPN) is a 7-tuple $EN = (P, T; F, D, W, S, G)$ where:

- (1) P is a finite set of places;
- (2) T is a finite set of transitions T such that $P \cap T = \emptyset$ and $P \cup T \neq \emptyset$;
- (3) $F \subseteq (P \times T) \cup (T \times P)$ is a set of directed arcs;
- (4) D is a finite, non-empty set of symbol strings denoting the types of tokens;
- (5) $W : F \rightarrow \langle a_1 d_1, a_2 d_2, a_3 d_3, \dots, a_l d_l \rangle, a_l \in \{0, 1\}, d_l \in D$, and $l > 0$ is the number of elements in D ;
- (6) $S \subset D$ denotes a set of key token types; and
- (7) $G : T \rightarrow \Pi$ is a predicate function that assigns a predicate to each transition $t \in T$ where Π is the set of Boolean expressions on D .

Definition 2 (Marking of EBPN). A marking of an EBPN $EN = (P, T; F, D, W, S, G)$ is $M : P \rightarrow \langle n_1 d_1, n_2 d_2, n_3 d_3, \dots, n_l d_l \rangle, n_l \in \mathbb{N} = \{0, 1, 2, \dots\}; d_l \in D$, and $l > 0$ is the number of data elements in D .

A marking M of an EBPN assigns k -dimensional vectors to places. The vector’s component $n_k d_k$ means that a place has n_k tokens belonging to type d_k . Here, a token is a trading parameter that belongs to some type in an EBPN.

Definition 3 (Data State). A pair (M, δ_D) is a data state of EN , if M is a marking of EN , and δ_D is called a data allocation which assigns a value **T** (true), or **F** (false) to each $d \in \{M(p) \mid p \in P\}$ such that $d \in (D - S) \rightarrow \delta_D(d) = \mathbf{T}$, and $\delta_D : S \rightarrow \{\mathbf{T}, \mathbf{F}\}$.

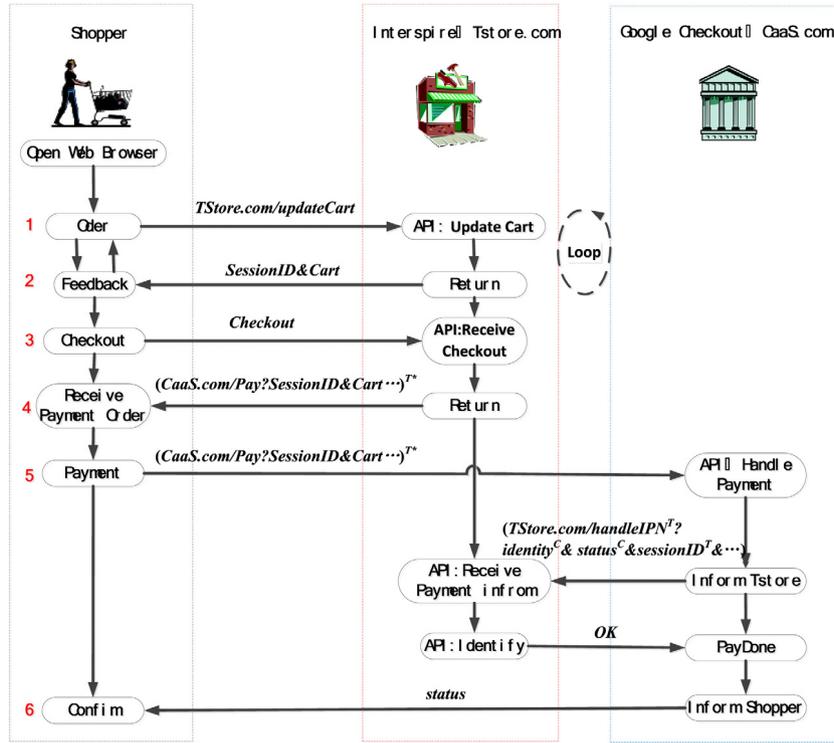


Fig. 1. Business process of integrating Interspire and Google Checkout.

Definition 4 (δ_G). δ_G is a Boolean function that assigns a Boolean value **T** (true) or **F** (false) to each $G(t)$ such that $\delta_G: G(t) \rightarrow \{\mathbf{T}, \mathbf{F}\}$, $t \in T$.

Definition 5 (Firing Conditions). A transition $t \in T$ is enabled at a data state $= (M, \delta_D)$ if

- (1) $\forall p \in \bullet t, M(p) \geq W(p, t)$; and
- (2) $\exists G(t) \rightarrow \delta_G(G(t)) = \mathbf{T}$.

Definition 6 (Key Transition). Given $t \in T$, $\bullet t = P$, and $t \bullet = P$, t is called a key transition if

- (1) $S \cap \{\tilde{W}(t, p) \mid p \in P''\} \neq \emptyset$; and
- (2) The token $s \in S \cap \{\tilde{W}(t, p) \mid p \in P''\}$ is produced by $t \rightarrow \delta_D(s) \in \{\mathbf{T}, \mathbf{F}\}$.

Definition 7 (Firing Rules). Let $EN = (P, T; F, D, W, S, G)$ be an EBPN, and $= (M, \delta_D)$ be a data state of EN . A transition $t \in T$, which is enabled at (M, δ_D) , can fire under M ($M \xrightarrow{t}$), and a new marking $M'(M \xrightarrow{t} M')$ is

$$M'(p) = \begin{cases} M(p) - W(p, t), & \text{if } p \in \bullet t - t \bullet \\ M(p) + W(t, p), & \text{if } p \in t \bullet - \bullet t \\ M(p) - W(p, t) + W(t, p), & \text{if } p \in \bullet t \cap t \bullet \\ M(p), & \text{otherwise.} \end{cases}$$

If t is not a key transition, a new data state is

$$\begin{aligned} \Delta' &= (M', \delta_{D'}) \\ &= (M', \forall d \in \{\tilde{M}(p) \mid p \in P\} \rightarrow \delta_{D'}(d) = \delta_D(d) \\ &\quad \wedge \forall d \in \{\tilde{W}(t, p) \mid p \in t \bullet\} - \{\tilde{M}(p) \mid p \in P\} \rightarrow \delta_{D'}(d) = \mathbf{T}). \end{aligned}$$

Else if t is a key transition, a new state set Γ is

$$\begin{aligned} \Gamma &= \{(M', \delta_{D'}) \mid M \xrightarrow{t} M', \\ &\quad \forall s \in \{\tilde{W}(t, p) \mid p \in t \bullet\} \cap S \rightarrow \delta_{D'}(s) \in \{\mathbf{T}, \mathbf{F}\}, \\ &\quad \forall d \in \{\tilde{M}(p) - \{\tilde{W}(t, p) \mid p \in t \bullet\} \cap S\} \rightarrow \delta_{D'}(d) = \delta_D(d)\}. \end{aligned}$$

Definition 8 (RD). Let (M_0, δ_{D0}) be the initial data state of $EN = (P, T; F, D, W, S, G)$. Its Reachability Data state graph (RD) can be defined as a 3-tuple $RD(EN) = (N, E; L)$, where

- (1) N is a set of nodes, $N = R(M_0, \delta_{D0})$;
- (2) E is a set of arcs, $E = \{(M_i, \delta_{Di}), (M_j, \delta_{Dj}) \mid (M_i, \delta_{Di}), (M_j, \delta_{Dj}) \in R(M_0, \delta_{D0}), \exists t_k \in T: (M_i, \delta_{Di}) \xrightarrow{t_k} (M_j, \delta_{Dj})\}$; and
- (3) $L: E \rightarrow T$, $L((M_i, \delta_{Di}), (M_j, \delta_{Dj})) = t_k$ if and only if $(M_i, \delta_{Di}) \xrightarrow{t_k} (M_j, \delta_{Dj})$, and t_k is called the label of the arc between (M_i, δ_{Di}) and (M_j, δ_{Dj}) . (M_j, δ_{Dj}) is the successor (node) of (M_i, δ_{Di}) , and (M_i, δ_{Di}) is the predecessor (node) of (M_j, δ_{Dj}) .

Definition 9 (Three-dimensional Incidence Matrix). Let $EN = (P, T; F, D, W, S, G)$ be an EBPN, $P = \{p_1, p_2, \dots, p_m\}$, $T = \{t_1, t_2, \dots, t_n\}$, $D = \{d_1, d_2, \dots, d_l\}$, $m, n, l \in \mathbb{N}^+ = \{1, 2, \dots\}$; then the static structure of EN can be expressed by a three-dimensional incidence matrix $\Psi = [\psi_{ijk}]_{n \times m \times l}$, where $\psi_{ijk} = \psi_{ijk}^+ - \psi_{ijk}^-$

$$\psi_{ijk}^+ = \begin{cases} W(t_i, p_j)_k, & \text{if } (t_i, p_j) \in F, i \in \{1, 2, \dots, n\}, \\ & j \in \{1, 2, \dots, m\}, k \in \{1, 2, \dots, l\} \\ \text{an } l\text{-dimensional } \mathbf{0} \text{ vector } \langle 0, 0, \dots, 0 \rangle, & \text{otherwise} \end{cases}$$

$$\psi_{ijk}^- = \begin{cases} W(p_j, t_i)_k, & \text{if } (p_j, t_i) \in F, i \in \{1, 2, \dots, n\}, \\ & j \in \{1, 2, \dots, m\}, k \in \{1, 2, \dots, l\} \\ \text{an } l\text{-dimensional } \mathbf{0} \text{ vector } \langle 0, 0, \dots, 0 \rangle, & \text{otherwise.} \end{cases}$$

The above two equations can also be expressed as

$$\psi_{ij}^+ = \begin{cases} W(t_i, p_j), & \text{if } (t_i, p_j) \in F, i \in \{1, 2, \dots, n\}, \\ & j \in \{1, 2, \dots, m\} \\ \text{an } l\text{-dimensional } \mathbf{0} \text{ vector } \langle 0, 0, \dots, 0 \rangle, & \text{otherwise} \end{cases}$$

$$\psi_{ij}^- = \begin{cases} W(p_j, t_i), & \text{if } (p_j, t_i) \in F, i \in \{1, 2, \dots, n\}, \\ & j \in \{1, 2, \dots, m\} \\ \text{an } l\text{-dimensional } \mathbf{0} \text{ vector } \langle 0, 0, \dots, 0 \rangle, & \text{otherwise} \end{cases}$$

$$\psi_{ij} = \psi_{ij}^+ - \psi_{ij}^-.$$

In original Petri nets, two-dimensional incident matrix is defined by the relations of places and transitions. In EBPN, three-dimensional matrix is defined by the relations of places, transitions

and W . In Definition 9, $W(p_j, t_i)$ is an l -dimensional vector, and $W(p_j, t_i)_k$ is the k th scalar in $W(p_j, t_i)$. ψ is a notation of the element in Ψ . ψ_{ijk}^+ and ψ_{ijk}^- are scalars. ψ_{ij}^+ and ψ_{ij}^- are l -dimensional vectors.

Lemma 1. Let $EN = (P, T; F, D, W, S, G)$ be an EBPN, (M_0, δ_{D0}) be the initial data state, Ψ be the three-dimensional incidence matrix of EN , and $(M, \delta_D) \in R(M_0, \delta_{D0})$. Transition $t_i \in T$ is enabled at M if $\forall p_j \in \bullet t$ and $\forall k \in \mathbb{N}_l = \{1, 2, \dots, l\} \rightarrow M(p_j)_k \geq \psi_{ijk}^-$, i.e., $M(p_j) \geq \psi_{ij}^-$.

Definition 10 (Ψ^T). Let $EN = (P, T; F, D, W, S, G)$ be an EBPN, $\Psi = [\psi_{ijk}]_{n \times m \times l}$ is the three-dimensional incidence matrix. $\Sigma = \Psi^T$ is the transpose of Ψ , i.e., $\varepsilon_{ij} = \psi_{ji}$, where ε is an element in Σ .

Lemma 2. Let $EN = (P, T; F, D, W, S, G)$ be an EBPN, (M_0, δ_{D0}) be the initial data state, $(M, \delta_D) \in R(M_0, \delta_{D0})$, and Ψ be the three-dimensional incidence matrix of EN . If $t_i \in T$, $M \xrightarrow{t_i} M'$, then $M' = M + (\Psi_{i*})^T$.

Theorem 1. Let $EN = (P, T; F, D, W, S, G)$ be an EBPN, (M_0, δ_{D0}) be the initial data state, and Ψ be the three-dimensional incidence matrix of EN . If $(M, \delta_D) \in R(M_0, \delta_{D0})$, then there exists an n -dimensional non-negative integer vector V , such that $M = M_0 + \Psi^T V$.

Corollary 1. Let $EN = (P, T; F, D, W, S, G)$ be an EBPN, (M_0, δ_{D0}) be the initial data state, and Ψ be the three-dimensional incidence matrix of EN . There exist $(M_0, \delta_{D0}) \xrightarrow{\sigma} (M, \delta_D)$ and a n -dimensional non-negative integer vector V , such that $M = M_0 + \Psi^T V$. Then $\#(t_i, \sigma) = V[i]$, where $i \in \mathbb{N}_n = \{1, 2, \dots, n\}$, $n = |T|$, and $\#(t_i, \sigma)$ means the number of occurrences of t_i in σ .

4. Structural security

Structural security issues are derived from the design of business structures. Hybrid web applications that combine multiple participants into integrated services like e-commerce websites have rapidly developed, and bring in new security concerns. The structural integration of multiple participants introduces new security challenges due to the complexity of an application to coordinate its internal states with those of the component services and web client across the Internet [3,4]. As the new security challenges of e-commerce business processes are at the application-level, structural security is beyond the capabilities of network-level and operating system-level security approaches. Even though the traditional security requirements are satisfied, there are still many structure and logic flaws at the design level of business processes [25,26].

Formal methods are mathematical techniques for specifying and verifying correctness and trustworthiness of software systems. Consequently, we use the formal model-EBPN to model e-commerce business processes and verify the structural security based on behavioral sequence and state analyzing methods. Fig. 2 shows the framework. Given the specification of an e-commerce business process, including development documents, UML diagrams, and function specifications, we can model the business process by define control and data structures using EBPN. Then, verification methods are proposed based on dynamic properties of EBPN. Two methods can be used to analyze structural security issues of an e-commerce business process. One is behavioral sequence method, and the other is incidence matrix method. The related definitions of structural security:-

Proposition 1. Let \mathfrak{R} be a structural specification of an e-commerce business process, and $EN = (P, T; F, D, W, S, G)$ is an EBPN corresponding to \mathfrak{R} , (M_0, δ_{D0}) be the initial data state; γ is an illegal

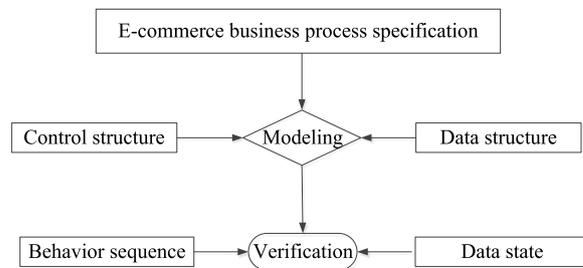


Fig. 2. Framework of this paper.

behavior sequence derived from \mathfrak{R} , and σ is a behavior sequence corresponding to γ . If $(M_0, \delta_{D0}) \xrightarrow{\sigma}$, then we call EN does not satisfy structural security.

Proposition 2. Let \mathfrak{R} be a structural specification of an e-commerce business process, and $EN = (P, T; F, D, W, S, G)$ is an EBPN corresponding to \mathfrak{R} , (M_0, δ_{D0}) be the initial data state, (M, δ_D) is an illegal data state constructed according to \mathfrak{R} ; If there is a behavioral sequence σ making that $(M_0, \delta_{D0}) \xrightarrow{\sigma} (M, \delta_D)$, then we call EN does not satisfy structural security.

5. Modeling methods

Here we define control and data structures for constructing an e-commerce business process; these depict the situation that several APIs or operation events fire one after another. A completed model for integrating control and data structures from a global viewpoint is then obtained. The benefit of which is to provide different views of a composite business process, which helps designers or users understand and analyze the e-commerce business process.

Definition 11. Suppose that $EN_1 = (P_1, T_1; F_1, D_1, W_1, S_1, G_1)$ and $EN_2 = (P_2, T_2; F_2, D_2, W_2, S_2, G_2)$ are two nets satisfying Definition 1, $P_1 \cap P_2 \neq \emptyset$, $T_1 \cap T_2 \neq \emptyset$, $F_1 \cap F_2 = \emptyset$, $D_1 \cap D_2 = \emptyset$, and $S_1 \cap S_2 = \emptyset$. Their composition is $EN = EN_1 \oplus EN_2 = (P_1 \cup P_2, T_1 \cup T_2, F_1 \cup F_2, D_1 \cup D_2, W, S_1 \cup S_2, G) = (P, T; F, D, W, S, G)$, in which for $\forall f_1 \in F_1 \subseteq F, W_1(f_1) = W(f_1); \forall f_2 \in F_2 \subseteq F, W_2(f_2) = W(f_2); \forall t_1 \in T_1 \subseteq T, G_2(t_1) = G(t_1);$ and $\forall t_2 \in T_2 \subseteq T, G_2(t_2) = G(t_2)$.

Definition 11 specifies a synthesis method of EBPN. In this work, we use it to synthesize control and data structures. To build up an e-commerce business process, we elicit intended functions in terms of design specifications and construct the EBPN according to some rules. Specific modeling rules are given as follows:

(1) Obtain the trading parameter set. Derive the trading parameter set involved in the design specifications and make D of the EN to be established;

(2) Construct the control structure models $EN_i = (P_i, T_i; F_i, D_i, W_i, S_i, G_i), i \in \mathbb{N}$, which correspond to Shopper, Merchant, and Caas, and so on. Identify the order of APIs and operation events in the e-commerce system according to key functionalities and design specifications, they are represented as transitions; connect them by using places and arcs;

(3) Construct a data structure model $EN_j = (P_j, T_j; F_j, D_j, W_j, S_j, G_j), j \in \mathbb{N}$. Identify the data flows and specify the input and output trading parameters of identified transitions; connect the transitions according to data flow specifications by using places and arcs;

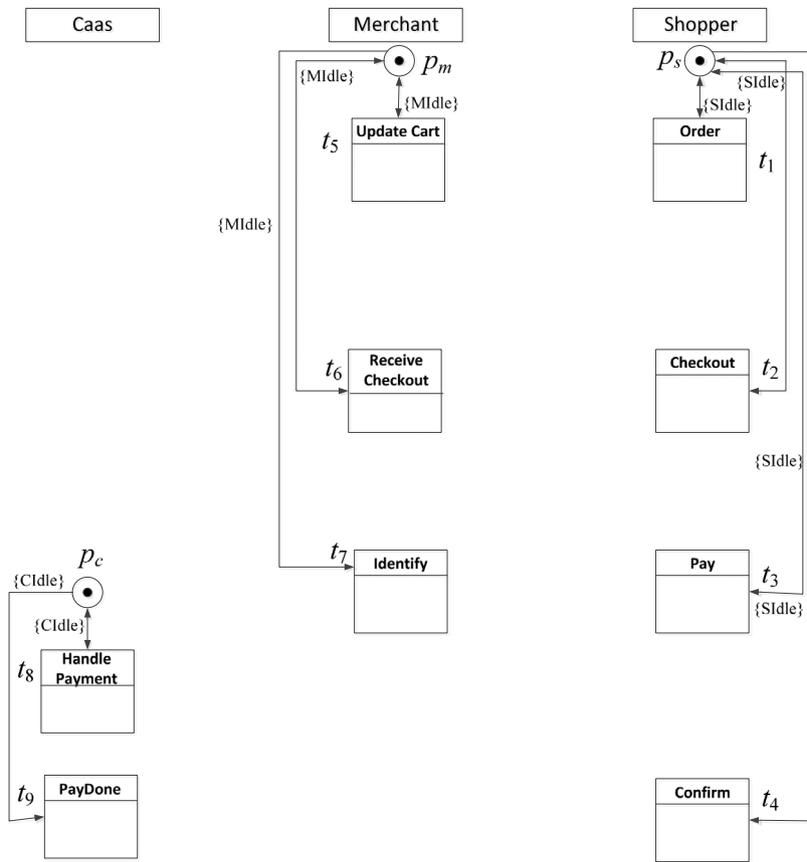


Fig. 3. Control structures of motivation example.

(4) Composing the control and data structures to obtain $EN = EN_{i1} \ominus EN_{i2} \ominus \dots \ominus EN_{in} \ominus \dots \ominus EN_j = (P, T; F, D, W, S, G)$, in which $i, 1, i, 2, in, j \in \mathbb{N}$;

(5) Add the initial data state. For an EBPN corresponding to an e-commerce business process, the initial data state is unique, which represents that multiple participants are ready for a deal.

Above steps describe the process of constructing an EBPN model. Using the proposed modeling methods and intended function specifications in Fig. 1 and Table 1, we can model the business process structures. For example, Fig. 3 depicts three control structures. The operation events of Shopper, as well as APIs of Caas and Merchant, are depicted by transitions. As Fig. 3 shows, the operation “Order” of Shopper is represented by t_1 , and the phrase in it is used to signal its function. t_5 is an API of Merchant, representing the function of processing an order from Shopper. In Fig. 3, p_s, p_m and p_c are the initial places of Shopper, Merchant and Caas respectively, and they are linked with three transitions: t_1, t_5 and t_8 via two contrary arrows. $\{Sidle, Middle, Cidle\}$ is the set of control parameters and this means that three participants are always ready to start a new transaction.

Fig. 4 is the data structure. $\{Cart, SessionID, Checkout, Status\}$ is the set of trading parameters. In the motivation example, only when the merchant is informed by the CaaS, the merchant will create an order of the transaction according to what is inside the cart and set its status to “PAID”, as per Table 1. API Handle Payment loads the cart directly from the shopper’s session, rather than from the CaaS, to build the order. This business function is represented by the place p_2 in data structure in Fig. 4. After the function of Update cart is done, t_5 would send three tokens with the types of $SessionID, Cart, Checkout$ respectively to p_2 . The arc from p_2 to

t_7 means that Merchant loads the cart directly from the shopper’s session.

Synthesize data and control structural models sequentially to obtain the complete EBPN (Fig. 5). Then, its initial marking $M_0 = [p_s(Sidle), p_m(Midle), p_c(Cidle), p_2(SessionID, Cart)]$ representing that multiple participants are ready to conduct a transaction. Note that, in this case, S and G are not used. In the following, we use bold zero ($\mathbf{0}$) to represent the l -dimensional 0 vector for clarity. The order of parameters in three-dimensional incidence matrix [23] is $\{Sidle, Middle, Cidle, Cart, SessionID, Checkout, Status\}$, and the numeric initial marking is $M_0 = [\langle 1, 0, 0, 0, 0, 0, 0 \rangle, \langle 0, 1, 0, 0, 0, 0, 0 \rangle, \langle 0, 0, 1, 0, 0, 0, 0 \rangle, \mathbf{0}, \langle 0, 0, 0, 1, 1, 0, 0 \rangle, \mathbf{0}, \mathbf{0}, \mathbf{0}, \mathbf{0}, \mathbf{0}, \mathbf{0}, \mathbf{0}$].

6. Analyzing structural security

We analyze structural security by two ways according to Propositions 1 and 2. One is the behavioral sequence method, in which illegal behavior sequences are constructed and executed to verify the structural security of an e-commerce business process; the other one is the state analyzing method, in which an illegal state is constructed and analyzed by three-dimensional incidence matrix.

6.1. Behavioral sequence method

By analyzing the case of e-commerce business process, we should construct the illegal behaviors that result in security issues. Then, convert them to the behavioral sequence of EBPN model. At last, executing them and determine whether it can be executed successfully. If yes, the business structures have problems; if no, the business structures are immune to these illegal behaviors.

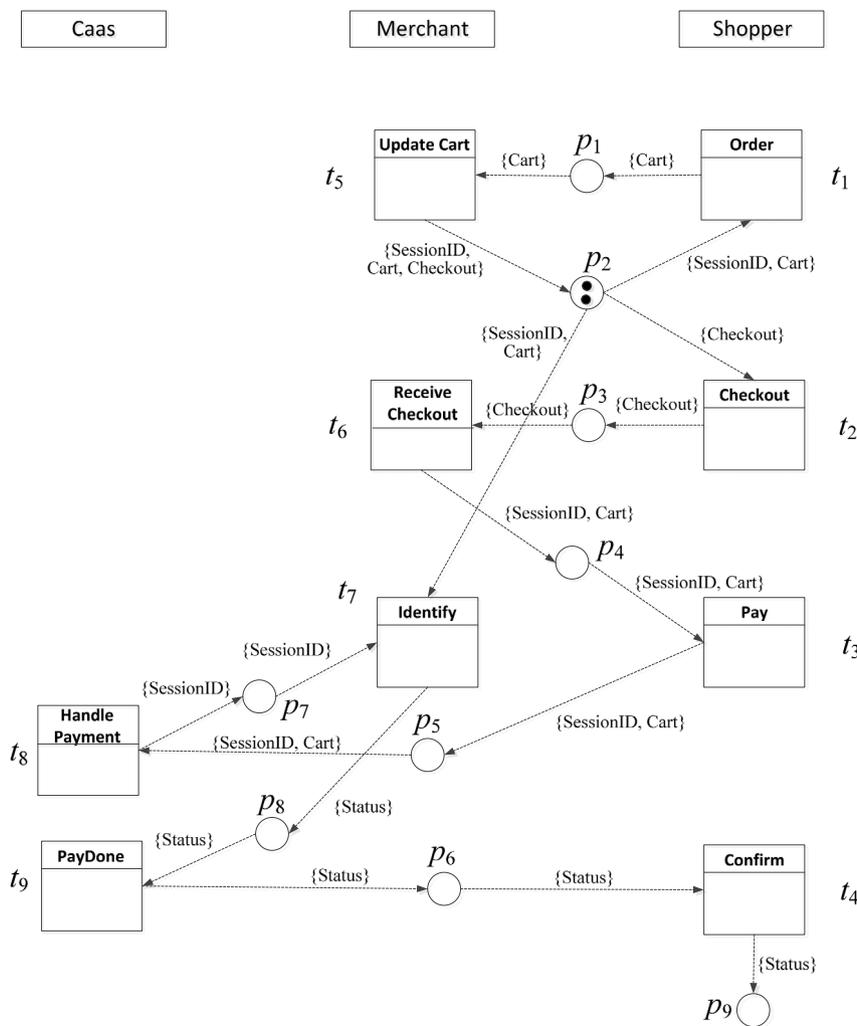


Fig. 4. Data structure of motivation example.

First, we should construct the illegal behavior specifications from the cases. Illegal behavior specification is a description of illegal behaviors in the case. For example, in the case of motivation example, the illegal behavior specification is:

$(\text{Order} \rightarrow \text{Update Cart})^* \rightarrow \text{Checkout} \rightarrow \dots \rightarrow (\text{Order} \rightarrow \text{Update Cart})^* \rightarrow \dots \rightarrow \text{Identify} \rightarrow \dots$

The notation $()^*$ means the loop executing of some events. The notation “...” means any executing events or transitions in the business process.

Definition 12. Suppose that $EN = (P, T; F, D, W, S, G)$ is an EBPN model, the illegal behavior sequence σ can be defined as follows:

- (1) $t \in T$ can be an illegal behavior sequence;
- (2) $t_1 t_2 \dots t_n$ can be an illegal behavior sequence, $n \in \mathbb{N}^+$;
- (3) $(t_1 t_2 \dots t_n)^*$ can be an illegal behavior sequence;
- (4) The composition of (1)–(3) can be an illegal behavior sequence.

Thus, the corresponding illegal behavior sequence of above illegal behavior specifications is:

$(t_1 t_5)^* t_2 \dots (t_1 t_5)^* \dots t_7 \dots$

Then, we should conclude a specific behavior sequence according to illegal behavior sequence. For example, according to Fig. 5 and the illegal behavior sequence, we can get a specific behavior sequence $t_1 t_5 t_2 t_1 t_5 t_6 t_3 t_8 t_7$. Using the dynamic properties of

EBPN, execute the sequence and the executing process is shown in Fig. 6. The specific behavioral sequence can be executed successfully, and the business structures of motivation example do not satisfy structural security.

6.2. State analyzing method

In addition, we can use the states method to analyze structural security. First, we need to construct an illegal data state according to the structural security issue. Then, determine the reachability of the illegal data state using a three-dimensional incidence matrix. If yes, there is a structural security problem in the e-commerce business process; if no, the e-commerce business process is immune to the structural security issue.

Then, we give the steps of determining the reachability of a data state (M, δ_D) in an EBPN $EN = (P, T; F, D, W, S, G)$ under the initial data state (M_0, δ_0) .

- (1) Construct Ψ ;
- (2) According to Theorem 1, compute whether the non-negative integer n -dimensional vector V exists;
- (3) If not so, conclude that (M, δ_D) is not reachable in EN under the initial data state (M_0, δ_0) .
- (4) If V exists and the transition sequences σ such that $M_0 \xrightarrow{\sigma} M$ can be found, executing σ in EN , and the reachability of (M, δ_D) can be determined.

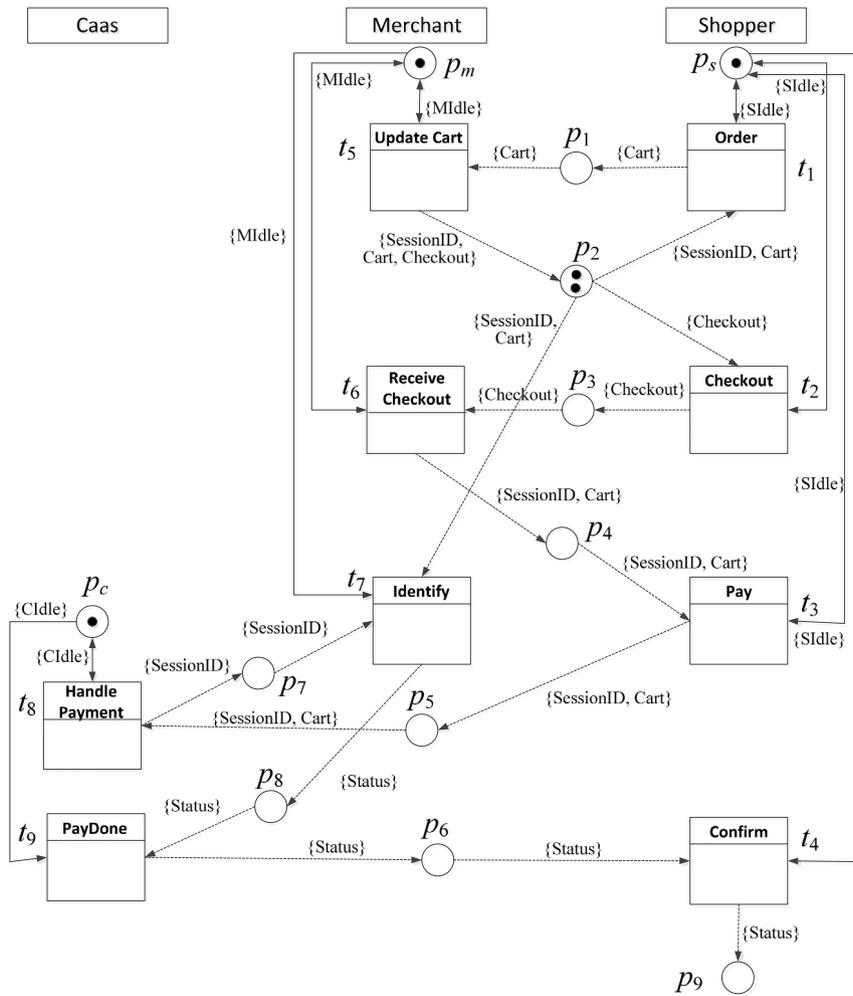


Fig. 5. Complete business structure of motivation example.

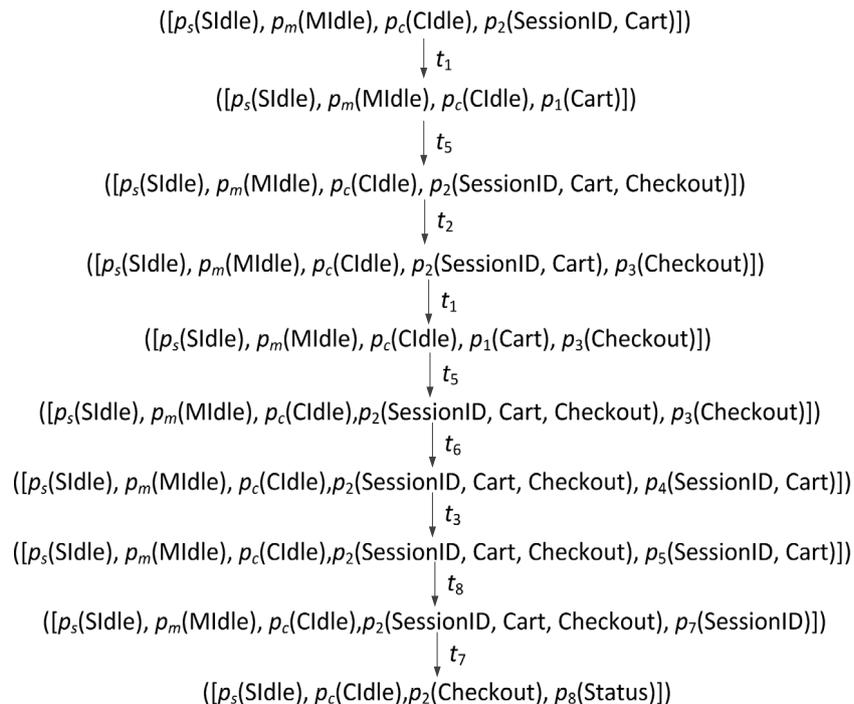


Fig. 6. Executing process of the specific behavioral sequence.

$$\begin{bmatrix} \langle 1, 0, 0, 0, 0, 0, 0 \rangle \\ \langle 0, 1, 0, 0, 0, 0, 0 \rangle \\ \langle 0, 0, 1, 0, 0, 0, 0 \rangle \\ \langle 0, 0, 0, 1, 0, 0, 0 \rangle \\ \mathbf{0} \\ \langle 0, 0, 0, 0, 0, 1, 0 \rangle \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \end{bmatrix} = \begin{bmatrix} \langle 1 - V[4], 0, 0, 0, 0, 0, 0 \rangle \\ \langle 0, 1 - V[7], 0, 0, 0, 0, 0 \rangle \\ \langle 0, 0, 1 - V[9], 0, 0, 0, 0 \rangle \\ \langle 0, 0, 0, V[1] - V[5], 0, 0, 0 \rangle \\ \langle 0, 0, 0, 1 - V[1] + V[5] - V[7], 1 - V[1] + V[5] - V[7], 0 - V[2] + V[5], 0 \rangle \\ \langle 0, 0, 0, 0, 0, V[2] - V[6], 0 \rangle \\ \langle 0, 0, 0, V[6] - V[3], V[6] - V[3], 0, 0 \rangle \\ \langle 0, 0, 0, V[3] - V[8], V[3] - V[8], 0, 0 \rangle \\ \langle 0, 0, 0, 0, 0, 0, V[9] - V[4] \rangle \\ \langle 0, 0, 0, 0, 0, 0, V[8] - V[7] \rangle \\ \langle 0, 0, 0, 0, 0, 0, V[7] - V[9] \rangle \\ \langle 0, 0, 0, 0, 0, 0, V[4] \rangle \end{bmatrix}$$

Box I.

In the case of motivation example, we can obtain the illegal data state $(M, \delta_D) = ([p_s(SIdle), p_m(Midle), p_c(CIdle), p_1(Cart), p_3(Checkout)])$, and it means that Shopper has send the message of Checkout. However, he/she update the cart again. This is not allowed in a security e-commerce business process. First, we construct three-dimensional incidence matrix of the EBPN model. Ψ^+ and Ψ^- of the EN in Fig. 5 is shown in Table A.1, Table A.2 in Appendix. Then, according to Definition 9, $\Psi = \Psi^+ - \Psi^-$ is shown in Table A.3 in Appendix, where $\Psi^+ = [\psi_{ijk}^+]_{n \times m \times l}$, and $\Psi^- = [\psi_{ijk}^-]_{n \times m \times l}$. The non-simplified $M = [\langle 1, 0, 0, 0, 0, 0, 0 \rangle, \langle 0, 1, 0, 0, 0, 0, 0 \rangle, \langle 0, 0, 1, 0, 0, 0, 0 \rangle, \langle 0, 0, 0, 1, 0, 0, 0 \rangle, \mathbf{0}, \langle 0, 0, 0, 0, 0, 1, 0 \rangle, \mathbf{0}, \mathbf{0}, \mathbf{0}, \mathbf{0}, \mathbf{0}, \mathbf{0}, \mathbf{0}$. Therefore, for (M, δ_D) , the matrix equation can be:

$$\begin{bmatrix} \langle 1, 0, 0, 0, 0, 0, 0 \rangle \\ \langle 0, 1, 0, 0, 0, 0, 0 \rangle \\ \langle 0, 0, 1, 0, 0, 0, 0 \rangle \\ \langle 0, 0, 0, 1, 0, 0, 0 \rangle \\ \mathbf{0} \\ \langle 0, 0, 0, 0, 0, 1, 0 \rangle \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \end{bmatrix} = \begin{bmatrix} \langle 1, 0, 0, 0, 0, 0, 0 \rangle \\ \langle 0, 1, 0, 0, 0, 0, 0 \rangle \\ \langle 0, 0, 1, 0, 0, 0, 0 \rangle \\ \mathbf{0} \\ \langle 0, 0, 0, 1, 1, 0, 0 \rangle \\ \mathbf{0} \end{bmatrix} + \Psi^T \begin{bmatrix} V[1] \\ V[2] \\ V[3] \\ V[4] \\ V[5] \\ V[6] \\ V[7] \\ V[8] \\ V[9] \end{bmatrix}$$

Solve the equation and one step of the process is given in Box I. Then, to obtain the unique solution $V = [V[1], V[2], V[3], V[4], V[5], V[6], V[7], V[8], V[9]]^T = [2, 1, 0, 0, 1, 0, 0, 0, 0]^T$. According to Corollary 1, it is easy to find a sequence $\sigma = t_1 t_5 t_2 t_1$ such that $M_0 \xrightarrow{\sigma} M$. Then, execute σ in Fig. 5, and the executing process is shown in Fig. 3. By analyzing Fig. 6, we conclude that $(M, \delta_D) = ([p_s(SIdle), p_m(Midle), p_c(CIdle), p_1(Cart), p_3(Checkout)])$ is reachable from initial data state. This means the business structure in Fig. 5 has some problems, and we can find the problem and correct it. Fig. 7 shows the correct structures and has no structure security issue in the motivation example.

Table A.1 Ψ^+ of Fig. 5.

p_i	p_m	p_c	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	
$\langle 1, 0, 0, 0, 0, 0, 0 \rangle$	0	0	$\langle 0, 0, 0, 1, 0, 0, 0 \rangle$	0	0	0	0	0	0	0	0	t_1
$\langle 1, 0, 0, 0, 0, 0, 0 \rangle$	0	0	0	0	$\langle 0, 0, 0, 0, 1, 0 \rangle$	0	0	0	0	0	0	t_2
$\langle 1, 0, 0, 0, 0, 0, 0 \rangle$	0	0	0	0	0	0	$\langle 0, 0, 0, 1, 1, 0, 0 \rangle$	0	0	0	0	t_3
0	0	0	0	0	0	0	0	0	0	0	$\langle 0, 0, 0, 0, 0, 0, 1 \rangle$	t_4
0	$\langle 0, 1, 0, 0, 0, 0, 0 \rangle$	0	0	$\langle 0, 0, 0, 1, 1, 1, 0 \rangle$	0	0	0	0	0	0	0	t_5
0	$\langle 0, 1, 0, 0, 0, 0, 0 \rangle$	0	0	0	0	$\langle 0, 0, 0, 1, 1, 0, 0 \rangle$	0	0	0	0	0	t_6
0	0	0	0	0	0	0	0	0	0	0	$\langle 0, 0, 0, 0, 0, 0, 1 \rangle$	t_7
0	0	$\langle 0, 0, 1, 0, 0, 0, 0 \rangle$	0	0	0	0	0	0	$\langle 0, 0, 0, 0, 1, 0, 0 \rangle$	0	0	t_8
0	0	0	0	0	0	0	0	$\langle 0, 0, 0, 0, 0, 0, 1 \rangle$	0	0	0	t_9

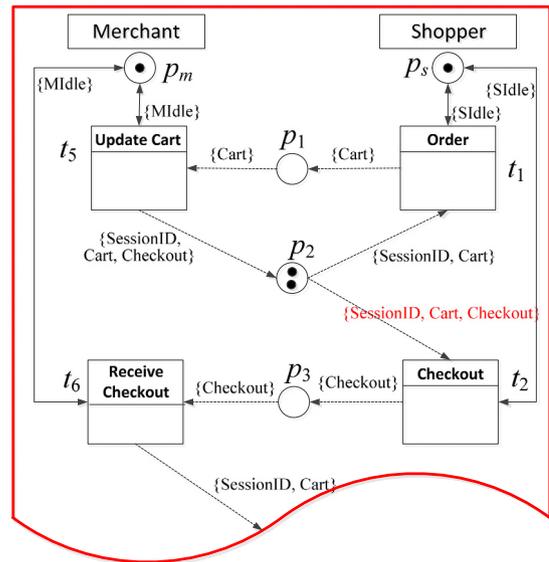


Fig. 7. Correct business structure of motivation example.

7. Conclusions

The rapid development of e-commerce has led to arise structural security issues in business processes. Based on EBPN, this paper discusses the concept of structural security and proposed a modeling method that fuses control and data structures. We propose two analyzing methods to determine the structural security of e-commerce business processes. However, plenty of analyzing methods in this area is still largely open. Even with the deployment of the proposed methods, there is still ample opportunity to conduct further research using additional analytical methods in structural security. In the future, we will focus on more efficient

Table A.2
 Ψ^- of Fig. 5.

p_s	p_m	p_c	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9
$\langle 1,0,0,0,0,0,0 \rangle$	0	0	0	$\langle 0,0,0,1,1,0,0 \rangle$	0	0	0	0	0	0	t_1
$\langle 1,0,0,0,0,0,0 \rangle$	0	0	0	$\langle 0,0,0,0,0,1,0 \rangle$	0	0	0	0	0	0	t_2
$\langle 1,0,0,0,0,0,0 \rangle$	0	0	0	0	0	$\langle 0,0,0,1,1,0,0 \rangle$	0	0	0	0	t_3
$\langle 1,0,0,0,0,0,0 \rangle$	0	0	0	0	0	0	0	$\langle 0,0,0,0,0,1 \rangle$	0	0	t_4
0	$\langle 0,1,0,0,0,0,0 \rangle$	0	$\langle 0,0,0,1,0,0,0 \rangle$	0	0	0	0	0	0	0	t_5
0	$\langle 0,1,0,0,0,0,0 \rangle$	0	0	0	$\langle 0,0,0,0,0,1,0 \rangle$	0	0	0	0	0	t_6
0	$\langle 0,1,0,0,0,0,0 \rangle$	0	0	$\langle 0,0,0,1,1,0,0 \rangle$	0	0	0	0	$\langle 0,0,0,0,1,0,0 \rangle$	0	t_7
0	0	$\langle 0,0,1,0,0,0,0 \rangle$	0	0	0	0	$\langle 0,0,0,1,1,0,0 \rangle$	0	0	0	t_8
0	0	$\langle 0,0,1,0,0,0,0 \rangle$	0	0	0	0	0	0	0	$\langle 0,0,0,0,0,0,1 \rangle$	t_9

Table A.3
 Ψ of Fig. 5.

p_s	p_m	p_c	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	
0	0	0	$\langle 0,0,0,1,0,0,0 \rangle$	$\langle 0,0,0,-1,-1,0,0 \rangle$	0	0	0	0	0	0	t_1	
0	0	0	0	$\langle 0,0,0,0,-1,0 \rangle$	$\langle 0,0,0,0,0,1,0 \rangle$	0	0	0	0	0	t_2	
0	0	0	0	0	0	$\langle 0,0,0,-1,-1,0,0 \rangle$	$\langle 0,0,0,1,1,0,0 \rangle$	0	0	0	t_3	
$\langle -1,0,0,0,0,0,0 \rangle$	0	0	0	0	0	0	0	$\langle 0,0,0,0,0,-1 \rangle$	0	0	$\langle 0,0,0,0,0,0,1 \rangle$	t_4
0	0	0	$\langle 0,0,0,-1,0,0,0 \rangle$	$\langle 0,0,0,1,1,1,0 \rangle$	0	0	0	0	0	0	t_5	
0	0	0	0	0	$\langle 0,0,0,0,-1,0 \rangle$	$\langle 0,0,0,1,1,0,0 \rangle$	0	0	0	0	t_6	
0	$\langle 0,-1,0,0,0,0,0 \rangle$	0	0	$\langle 0,0,0,-1,-1,0,0 \rangle$	0	0	0	0	$\langle 0,0,0,0,-1,0,0 \rangle$	$\langle 0,0,0,0,0,0,1 \rangle$	0	t_7
0	0	0	0	0	0	0	$\langle 0,0,0,-1,-1,0,0 \rangle$	$\langle 0,0,0,1,0,0,0 \rangle$	0	0	t_8	
0	0	$\langle 0,0,-1,0,0,0,0 \rangle$	0	0	0	0	0	$\langle 0,0,0,0,0,1 \rangle$	0	$\langle 0,0,0,0,0,-1 \rangle$	t_9	

analytical methods and deploy more technologies based on the original Petri nets.

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Appendix

See Tables A.1–A.3.

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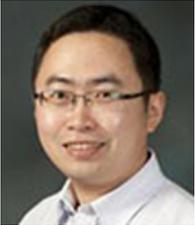
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