

# On the security of pairing-free certificateless digital signature schemes using ECC

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## Abstract

I cryptanalyze the pairing-free digital signature scheme of Islam et al. which is proven secure against “adaptive chosen message attacks”. I introduce this type of forgery to analyze their scheme. Furthermore, I comment on general security issues that should be considered when making improvements on their scheme. My security analysis is also applicable to other digital signatures designed in a similar manner.

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*Keywords:* Digital signature; Certificateless cryptography; Elliptic Curve cryptography; Random Oracle model; Provable security

## 1. Introduction

Certificateless public-key cryptography solves the certificate management problem in traditional public-key cryptography, and solves the key-escrow problem in identity-based public-key cryptography. There are numerous certificateless signature schemes [1–8], designed for different applications. To avoid bilinear pairing operations, Islam and Biswas [9] recently proposed a pairing-free certificateless digital signature scheme using elliptic curve cryptography (ECC). They also proved that their scheme was secure “against adaptive chosen-message and identity attacks” in the random oracle model. In this paper, I analyze the security of Islam et al.’s scheme and demonstrate that it is not secure even though it is proven secure against “adaptive chosen-message and identity attacks”. Furthermore, I comment on general security issues that should be considered when making improvements on their scheme. The security of other similar schemes can be checked using the same techniques, I employed in our study.

The remainder of this paper is organized as follows. In Section 2, we discuss the security problem in Islam et al.’s [9] scheme. Section 3 presents the security heal. Finally, Section 4 concludes the paper.

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## 2. Security analysis of Islam et al.’s scheme [9]

Adversary  $A$  can forge a valid signature on  $m$  by replacing the public key.

- After obtaining  $(ID_S, R_S)$ ,  $A$  randomly selects  $d_A, x_A \in \mathbb{Z}_q^*$ , computes  $P_A = x_A P$ ,  $H_0(ID_S, R_S, P_A)$ ,  $P'_{pub} = (d_A P - R_S)H_0^{-1}$  and replaces master public key  $P_{pub}$  with  $P'_{pub}$  and  $ID_S$ 's  $P_S$  with  $P_A$  so that  $d_A P = R_S + H_0(ID_S, R_S, P_A)P_{pub}'$  holds.
- $A$  sets  $(D_A, x_A)$  as full private key of the signer where  $D_A = (d_A, R_S)$ , and sets  $(P_A, R_S)$  as the full public key.
- To sign a message  $m \in \{0, 1\}^*$ ,  $A$  selects  $y_A \in_R \mathbb{Z}_q^*$ , computes  $Y_A = y_A P_A$ ,  $h_A = H_1(m, ID_S, R_S, Y_A)$  and  $t_A = H_2(m, ID_S, P_A, Y_A)$ .

Finally  $A$  computes  $\sigma_A = x_A y_A - (t_A x_A + h_A d_A) \bmod q$  and outputs the signature  $(\sigma_A, Y_A)$  on the message  $m$ .

Because  $Y_A = y_A P_A = y_A x_A P$ ,  $h_A = H_1(m, ID_S, R_S, Y_A)$ , and  $t_A = H_2(m, ID_S, P_A, Y_A)$ .

Thus,  $\sigma_A P = Y_A - t_A P_A - h_A (R_S + H_0(ID_S, P_A, R_S)P_{pub}')$ .

Therefore, the generated signature can pass the verification, and  $A$  generates a signature successfully.

## 3. Formal proof to heal the security

When designing a signature protocol such as the one described above, the system public key  $P_{pub}$  should be hashed

to eliminate the possibility of this type of forgery. A proposal to heal the security in [9] is given as follows.

- When executing Partial-Private-Key-Extract in [9], if  $P_{pub}$  is hashed in  $H_0$ , private key part  $d_i$  is computed as  $d_i = (r_i + x H_0(ID_i, R_i, P_i, P_{pub})) \bmod q$  so that the user can validate their partial private key tuple  $D_i = (d_i, R_i)$  by checking the equation  $d_i P = R_i + H_0(ID_i, R_i, P_i, P_{pub}) P_{pub}$ .
- Now, after obtaining  $(ID_S, R_S)$ , if  $A$  attempts to forge the signature in the same manner described in the previous section, it then randomly selects  $d_A, x_A \in Z_q^*$ , computes  $P_A = x_A P$ ,  $H_0(ID_S, R_S, P_A, P_{pub})$ ,  $P'_{pub} = (d_A P - R_S) H_0^{-1}$ , and replaces master public key  $P_{pub}$  with  $P'_{pub}$  and  $ID_S$ 's  $P_S$  with  $P_A$ .
- For the verification, one checks the equation  $d_A P = R_S + H_0(ID_S, R_S, P_A, P'_{pub}) P'_{pub}$ , which will not hold. Therefore, forgery is not possible.

One can check the security of other proposed schemes that employ designs similar to the one described above.

#### 4. Conclusion

In this paper, we have demonstrated that Islam et al.'s pairing-free certificate-less digital signature scheme is not secure against some forgery types even though it is proven secure against "adaptive chosen-message attacks". Furthermore,

we commented on security issues to present a counter-measure.

#### References

- [1] H. Chen, F.-T. Zhang, R.-S. Song, Certificateless proxy signature scheme with provable security, *J. Softw.* 20 (3) (2009) 692–701.
- [2] D. He, Y. Chen, J. Chen, A provably secure certificateless proxy signature scheme without pairings, *Math. Comput. Modelling* 57 (9-10) (2013) 2510–2518.
- [3] D. He, J. Chen, R. Zhang, An efficient and provably-secure certificateless signature scheme without bilinear pairings, *Int. J. Commun. Syst.* 25 (11) (2012) 1432–1442.
- [4] X. Li, K. Chen, L. Sun, Certificateless signature and proxy signature schemes from bilinear pairings, *Lith. Math. J.* 45 (1) (2005) 76–83.
- [5] R. Lu, D. He, C. Wang, Cryptanalysis and improvement of a certificateless proxy signature scheme from bilinear pairings, in: *Proceedings of the 8th ACIS International Conference on Software Engineering, Artificial Intelligence, Networking, and Parallel/Distributed Computing*, SNPD 07, Qingdao, China, July 2007, pp. 285–290.
- [6] S. Padhye, N. Tiwari, Ecdlp-based certificateless proxy signature scheme with message recovery, *Trans. Emerg. Telecommun. Technol.* (2012) <http://dx.doi.org/10.1002/ett.2608>.
- [7] H. Xiong, F. Li, Z. Qin, A provably secure proxy signature scheme in certificateless cryptography, *Informatica* 21 (2) (2010) 277–294.
- [8] L. Zhang, F. Zhang, Q. Wu, Delegation of signing rights using certificateless proxy signatures, *Inform. Sci.* 184 (2012) 298–309.
- [9] SK.-H. Islam, G.P. Biswas, Provable secure and pairing-free certificateless digital signature scheme using elliptic curve cryptography, *Int. J. Comput. Math.* 90 (11) (2013) 2244–2258.