



Contents lists available at ScienceDirect

Journal of Business Research



Forecasting incoming call volumes in call centers with recurrent Neural Networks

Mona Ebadi Jalal^{a,*}, Monireh Hosseini^a, Stefan Karlsson^b^a IT Department, Faculty of Industrial Engineering, K. N. Toosi University of Technology, Iran^b Faculty of Engineering (LTH), Lund University, Sweden

ARTICLE INFO

Article history:

Received 1 February 2016

Received in revised form 1 March 2016

Accepted 1 April 2016

Available online xxxx

Keywords:

Forecasting

Model prediction

Call center

Neural Networks

ABSTRACT

Researchers apply Neural Networks widely in model prediction and data mining because of their remarkable approximation ability. This study uses a prediction model based on the Elman and NARX Neural Network and a back-propagation algorithm for forecasting call volumes in call centers. The results can help determine the optimal number of agents necessary to reduce waiting time for customers, enabling profit maximization and reduction of unnecessary costs. This study also compares the performance of the Elman-NARX Neural Network model with the time-lagged feed-forward Neural Network in addressing the same problem. The experimental results indicate that the proposed method is efficient in forecasting the call volumes of call centers.

© 2016 Elsevier Inc. All rights reserved.

1. Introduction

Modern call centers are large and employ thousands of agents. Representing the front end of organizations, call centers are responsible for maintaining customer relationships and the overall public image of the organization. This study focuses on two important issues in call center operations:

First, call centers are labor-intensive, with the cost of agents generally comprising 60–80% of the overall operating budget (Aksin, Armony, & Mehrotra, 2007). Therefore, an effective management strategy must schedule a sufficient number of agents.

Second, call centers involve customer satisfaction factors such as perceived queuing time. Feinberg (Feinberg, Kim, Hokama, de Ruyter, & Keen, 2000) finds a statistically significant correlation between the length of queuing time and customer satisfaction, indicating that shorter queuing times have beneficial effects on customer satisfaction. Furthermore, according to Whiting and Donthu (2009), customer error in estimating queuing time affects their satisfaction. Consequently, shorter queuing times provide higher satisfaction than longer ones and avoid customer churn.

This study concludes that the first and most important step is to forecast future call volumes accurately.

Much literature exists on forecasting; however, few studies attempt to develop effective models to forecast incoming call volumes in call centers. This study proposes a Neural Network model for forecasting call volumes to reduce waiting times and determining the optimal number of agents.

Recently, the rapid development of artificial intelligence has contributed to the growth of several advanced algorithms that tackle a variety of analytical problems such as forecasting. An artificial Neural Network is a massively parallel-distributed processor of simple processing units, which has a natural propensity to store experimental knowledge and to make it available for use (Haykin, 1998). The main advantage of the Neural Network in comparison with classic linear methods is their ability to model functions characterized by non-linear dynamics. High adaptive ability, tolerance to various outer noises, and the influence of “heavy-tailed” distributions are other frequently mentioned advantages (Klevecka, 2011). Neural Networks have shown tremendous success in developing models that track the changes in the characteristics and parameters of a system (Adya & Callopy, 1998; Chen, Peng, & Wang, 2000; Dudul & Ghatol, 2004). Therefore, at any instant in time, Neural Network correctly simulates the given time-varying system, despite significant changes in the system's property, and perfectly mimics and identifies the actual physical system.

Considering these properties, this study addresses the problem of forecasting call volumes in a call center.

2. Neural Network models

Neural Network models developed as a generalization of the mathematical models of human cognition and neural biology. Some key attributes of the brain's information network include a nonlinear, parallel structure and dense connections between information nodes (Haykin, 1998). Neural Network models have proven successful in a variety of business fields such as accounting (Kuldeep & Sukanto, 2006; Landajo & de Andrés, 2007; Lenard, Alam, & Madey, 1995; Zhang, Cao, & Schniederjans, 2004), management information systems (Huang, Chiu, & Chen, 2008; Kuflik, Boger, & Shoval, 2006; Zhu, Premkumar, Zhang,

* Corresponding author.

E-mail addresses: m_ebadi_j@yahoo.com (M. Ebadi Jalal), hosseini@kntu.ac.ir (M. Hosseini), stefan.karlsson@plog.lth.se (S. Karlsson).

& Chu, 2001), marketing (Kim, Street, Russell, & Menczer, 2005; Thieme, Song, & Calanton, 2000), and production management (Al-Ahmari, 2008; Bhattacharyya, Sengupta, Mukhopadhyay, & Chattopadhyay, 2008; Das & Datta, 2007; Kaparthi & Suresh, 1994; Wang, Chen, & Lin, 2005; Wu, Chen, & Chian, 2006). However, when forecasting with Neural Networks, a major factor is that the goodness of results depends on its architecture.

2.1. Time-lagged feed-forward networks

Usually, researchers apply a special type of Neural Network known as a time-lagged feed-forward network in time series modeling and forecasting. A time-lagged feed-forward network is a powerful nonlinear filter consisting of a tapped delay memory and multilayer perceptron and the standard back-propagation algorithm is useful in training this type of Neural Networks (Haykin, 1998; Mozer, 1993).

2.2. Elman Neural Networks

The Elman Neural Network is a semi-recursive Neural Network that uses the back-propagation-through time learning algorithm to find patterns in value sequences. Elman Neural Network adds a layer to receive feedback from the network in the hidden layer as a step delay to the operator for purposes of memory; therefore, the system can adapt to time-varying characteristics, which directly reflects the dynamic process characteristics.

Further, the Elman Neural Network has better computing power than a feed-forward Neural Network; therefore, considering dynamic telephone traffic, Elman Neural Network is suitable to construct a nonlinear prediction model for the traffic time series data (Elman, 1990).

2.3. NARX Neural Networks

An important class of discrete-time nonlinear systems is the Nonlinear Auto-Regressive with eXogenous inputs (NARX) model (Chen, Billings, & Grant, 1990, Leontaritis & Billings, 1985, Ljung, 1987, Su & McAvoy, 1991, Su, McAvoy, & Werbos, 1992):

$$y(t) = f(y(t-1), \dots, y(t-D_y), u(t-1), \dots, u(t-D_u)) \tag{1}$$

where $u(t)$ and $y(t)$ represent input and output of the network at time t , D_u and D_y are the input and output order, and the function f is a nonlinear function. When the function f can be approximated by a Multilayer Perceptron, we call the resulting system a NARX recurrent Neural Network (Chen et al., 1990, Narendra & Parthasarathy, 1990).

3. Data and proposed model

3.1. Model specifications

Fig. 1 shows the proposed model that uses a combination of Elman Neural Network and NARX Neural Network. This study uses these networks because of their special abilities of forecasting. The Elman Neural Network can adapt to time-varying characteristics and find temporal patterns, which are important for forecasting call volumes. The NARX Neural Network stores information for long periods in the presence of noise; therefore, it has the ability to remove and ignore noises.

3.2. Data and forecasting accuracy procedure

The call volume data is from an Emdad Khodro Iran call center, which is a member of the Iran Khodro industrial group and complements IKCO's after sales services chain. Due to high call volumes and short-term forecasting, data collection was at random over a one-year period and a random selection is made of three months, and fifty days from these three months. Calculations for call volumes are for each

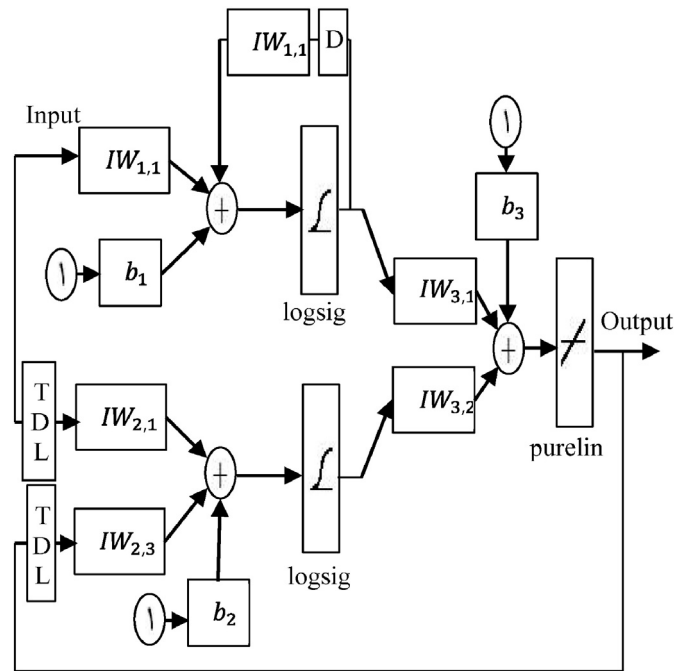


Fig. 1. Proposed model.

15-min case and 96 observations were made per day. Over fifty days, samples of 4800 observations were extracted from the raw data. Fig. 2 shows a scatter plot of call volumes per 15 min.

This study divides the data (4800 observations) into three parts (training, test, and check sets) to examine model performance. As per the standard method for train-and-test, this study removes 20% of the samples for testing and uses the remaining 80% for training (Thowmey & Smith, 1995). Further, the study uses 2% of the sample for checking, to prevent the problem of over-fitting. Therefore, 864 observations (test set) from the first 3840 (training set) are used to estimate the Neural Network weights of forecasting model and 96 observations (one day) to check it. After multiple iterations, the error is minimized thereby converging. The error signal can be given as:

$$e_i = d_i - y_i \tag{2}$$

where d_i is the targeted response and y_i is the actual output produced by the network response to input. The performance function used for the

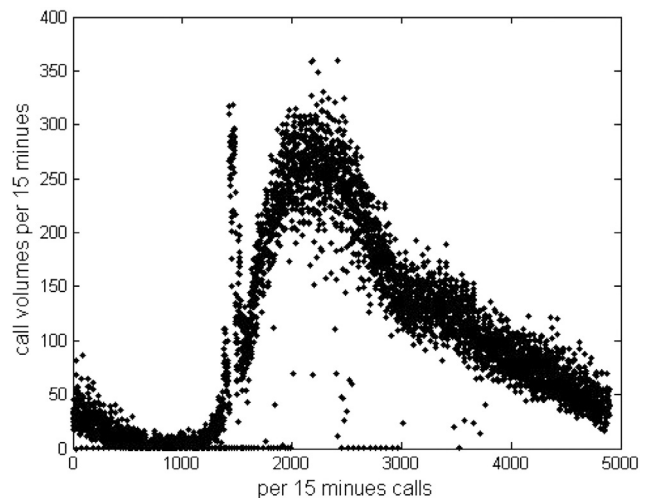


Fig. 2. The scatter plot of call volumes per 15 min.

Table 1
Results of proposed model.

Best topology	Number of epochs	MSE (train)	MSE (test)
4-5-6-1	50	2.9375e-05	4.9215e-04
4-5-6-1	100	2.6747e-05	7.0456e-05
4-5-6-1	300	1.2386e-05	5.5666e-06
4-5-6-1	500	1.8342e-06	3.3898e-07
4-5-6-1	700	5.5529e-06	2.0566e-06
4-5-6-1	1000	7.7055e-06	2.6239e-06

Notes: MSE denotes Mean Squared Error.

prediction model is the Mean Squared Error (MSE), which is the average squared error between the network outputs y_i and the targeted outputs d_i .

From Eq. (3), the MSE can be calculated as:

$$MSE = \frac{1}{n} \sum_{i=1}^n (x_i - \hat{x}_i)^2 \quad (3)$$

where x_i (\hat{x}_i) is the actual (forecasted) call volumes for period 15 min.

4. Results and discussion

Table 1 presents the results from the proposed model. The method was applied to several topologies of the Artificial Neural Network the one with the best performance was selected. Table 1 presents the average after obtaining 10 results on each topology. Note that the topologies 4-5-6-1 with 500 epochs show better performance (Minimum MSE) in comparison to other topologies.

As there were no capable models for forecasting incoming call volumes, this study compares the proposed model with a base model such as the time-lagged feed-forward network, which is a base model for short-term traffic forecasting using Neural Networks (Haykin, 1998; Mozer, 1993).

Table 2 presents the results from the time-lagged feed-forward network for call volume forecasting. As before, Table 2 presents the average of 10 results on each topology and topology after selecting the best performance. Note that the topologies 4-5-1 with 150 epochs show better performance in comparison to other topologies.

Table 2 shows that the over-fitting problem occurs when training the time-lagged feed-forward network with the dataset. These results indicate that the E-NARX Neural Network, which incorporates the advantages of the Elman and NARX networks forecasts more accurately than previous Neural Network models.

Fig. 3 shows a comparison for the best-fit model. The plot reveals that the proposed model follows the variation in the actual time series more closely than its rival model (?), which is also evident from its better performance statistics.

5. Concluding remarks

This study proposes and evaluates a recurrent Neural Network applied to actual call center data. The forecaster is a three-layer network,

Table 2
Time-lagged feed-forward network results.

Topology	Number of epochs	MSE (train)	MSE (test)
4-5-1	50	4.6678e-05	6.5524e-04
4-5-1	75	2.0664e-06	0.0352
4-7-1	100	1.4050e-06	0.02227
4-10-1	100	3.7132e-06	0.1843
4-15-1	100	2.7749e-06	0.0384
4-15-1	200	1.8890e-06	1.9577
4-15-1	500	6.7474e-05	0.9048

Notes: MSE denotes Mean Squared Error.

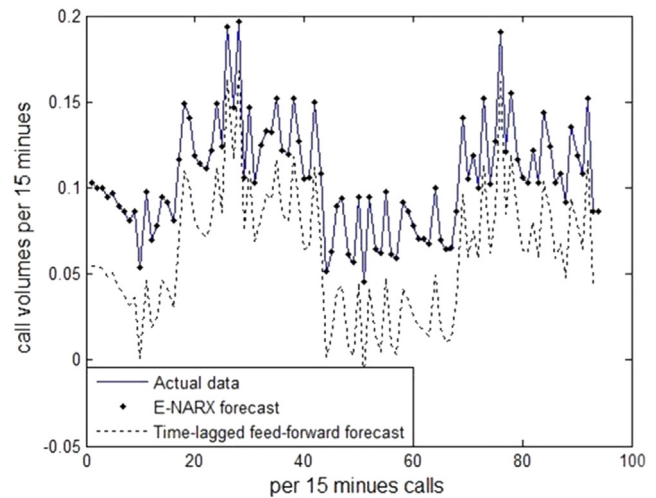


Fig. 3. Comparison of the forecasting ability of the proposed E-NARX forecaster with the best representative of the rival models.

which can find temporal patterns and store information for a long period in the presence of noise and is simulated using MATLAB software.

The results indicate that the proposed forecaster is a promising computational intelligence approach to the problem of forecasting incoming call volumes, since it is capable of capturing the time-series dynamics through special connections.

Forecasting might be a valuable tool for call center managers. Using historical data, managers may predict future demand by forecasting a reasonably accurate call volume. This study considers this useful in determining the optimal number of agents necessary to reduce waiting times for customers, either for profit maximization or for reducing unnecessary costs.

References

Adya, M., & Callopy, F. (1998). How effective are Neural Networks at forecasting prediction? A review and evaluation. *Journal of Forecasting*, 17, 481–495.

Aksin, Z., Armony, M., & Mehrotra, V. (2007). The modern call center: a multi-disciplinary perspective on operations management research. *Production and Operations Management*, 16(6), 665–688.

Al-Ahmari, A. (2008). Prediction and optimization models for turning operations. *International Journal of Production Research*, 46(15), 4061–4081.

Bhattacharyya, P., Sengupta, D., Mukhopadhyay, S., & Chattopadhyay, A. (2008). Online tool condition monitoring in face milling using current and power signals. *International Journal of Production Research*, 46(4), 1187–1201.

Chen, B. S., Peng, S. C., & Wang, K. C. (2000). Traffic modeling, prediction, and congestion control for high speed networks: A fuzzy AR approach. *IEEE Transactions on Fuzzy Systems*, 8(5), 491–508.

Chen, S., Billings, S. A., & Grant, P. M. (1990). Non-linear system identification using neural networks. *International Journal of Control*, 51(6), 1191–1214.

Das, P., & Datta, S. (2007). Exploring the non-linearity in empirical modelling of a steel system using statistical and neural network models. *International Journal of Production Research*, 45(3), 699–717.

Dudul, S. V., & Ghatol (2004). Identification of linear dynamical time invariant systems using feedforward neural network. *IE (I) Journal*, 84, 66–71.

Elman, J. L. (1990). Finding structure in time. *Cognitive Science*, 14, 179–211.

Feinberg, R. A., Kim, I., Hokama, L., de Ruyter, K., & Keen, C. (2000). Operational determinants of caller satisfaction in the contact center. *International Journal of Service Industry Management*, 11(2), 131–141.

Haykin, S. (1998). *Neural networks: A comprehensive foundation* (2nd ed.). Englewood Cliffs: Prentice Hall.

Huang, S., Chiu, N., & Chen, L. (2008). Integration of the grey relational analysis with genetic algorithm for software effort estimation. *European Journal of Operational Research*, 188(3), 898–909.

Kaparthi, S., & Suresh, N. (1994). Performance of selecting part-machine grouping technique for data sets of wide ranging sizes and imperfection. *Decision Sciences*, 25(4), 515–532.

Kim, Y., Street, N., Russell, G., & Menczer, F. (2005). Customer targeting: A neural network approach guided by genetic algorithms. *Management Science*, 51(2), 264–276.

Klevecka, I. (2011). Short-term traffic forecasting with neural networks. *Transport and Telecommunication*, 12(2), 20–27.

Kuflik, T., Boger, Z., & Shoval, P. (2006). Filtering search results using an optimal set of terms identified by an artificial neural network. *Information Processing and Management*, 42(2), 469–483.

- Kuldeep, K., & Sukanto, B. (2006). Artificial neural network vs. linear discriminant analysis in credit ratings forecast: A comparative study of prediction performances. *Review of Accounting & Finance*, 5(3), 216–227.
- Landajo, M., & de Andrés, J. (2007). Robust neural modeling for the cross-sectional analysis of accounting information. *European Journal of Operational Research*, 177(2), 1232–1252.
- Lenard, M., Alam, P., & Madey, G. (1995). The application of neural networks and a qualitative response model to the auditor's going concern uncertainty decision. *Decision Sciences*, 26(2), 209–224.
- Leontaritis, I. J., & Billings, S. A. (1985). Input–output parametric models for non-linear systems: Part I: Deterministic non-linear systems. *International Journal of Control*, 41(2), 303.
- Ljung, L. (1987). *System identification: theory for the user*. Englewood Cliffs, NJ: Prentice-Hall.
- Mozer, M. C. (1993). Neural network architectures for temporal pattern processing. In A. S. Weigend, & N. A. Gershenfeld (Eds.), *Time series prediction: Forecasting the future and understanding the past* (pp. 243–264). Perseus Book Publishing.
- Narendra, K. S., & Parthasarathy, K. (1990). Identification and control of dynamical systems using neural networks. *IEEE Transactions on Neural Networks*, 1(1), 4–27.
- Su, H. T., & McAvoy, T. J. (1991). Identification of chemical processes using recurrent networks. *Proceedings of the American Controls Conference*, 3. (pp. 2314–2319).
- Su, H. -T., McAvoy, T. J., & Werbos, P. (1992). Long-term predictions of chemical processes using recurrent neural networks: A parallel training approach. *Industrial Engineering and Chemical Research*, 31, 1338.
- Thieme, R., Song, M., & Calanton, R. (2000). Artificial neural network decision support systems for new product development project selection. *Journal of Marketing Research*, 37(2), 499–506.
- Thowmey, J. M., & Smith, A. E. (1995). Committee networks by resampling. *Intelligent Neural Engineering System through Artificial networks*, 6, 889–894.
- Wang, K., Chen, J., & Lin, Y. (2005). A hybrid knowledge discovery model using decision tree and neural network for selecting dispatching rules of a semiconductor final testing factory. *Production Planning and Control*, 16(7), 665–680.
- Whiting, A., & Donthu, N. (2009). Closing the gap between perceived and actual waiting times in a contact center: Results from a field study. *Journal of Services Marketing*, 23(5), 279–288.
- Wu, R., Chen, R., & Chian, S. (2006). Design of a product quality control system based on the use of data mining techniques. *IIE Transactions*, 38(1), 39–51.
- Zhang, W., Cao, Q., & Schniederjans, M. (2004). Neural network earnings per share forecasting models: A comparative analysis of alternative methods. *Decision Sciences*, 35(2), 205–237.
- Zhu, D., Premkumar, G., Zhang, X., & Chu, C. (2001). Data mining for network intrusion detection: A comparison of alternative methods. *Decision Sciences*, 32(4), 635–653.