Spectral features extraction for estimation of soil total nitrogen content based on modified ant colony optimization algorithm

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ABSTRACT
Nondestructive and rapid estimation of soil total nitrogen (TN) content by using near-infrared spectroscopy plays a crucial role in agriculture. The obtained original spectrum, however, presents several disadvantages, such as high redundancy, large computation, and complex model, because it generally processes a large amount of data. This study aimed to determine soil TN content-sensitive wavebands with high information quality, considerable predictive ability, and low redundancy. This paper proposes an evaluation criterion in selecting sensitive wavebands based on three factors, namely, degree of relevance with target variables, representative ability of the entire spectral information, and redundancy of the selected wavebands. Based on these three factors, two methods, namely, mutual information (MI) algorithm and the combination of ant colony optimization (ACO) and MI, were innovatively developed to identify soil TN content-sensitive wavebands. After the analysis and comparison, a set of wavebands, including 943, 1004, 1097, 1351, 1550, 1710, 2123, and 2254 nm, using the ACO-MI combined method was selected as the soil TN content-sensitive wavebands to estimate the TN content of soil samples, under four soil types, collected from different regions. The partial least squares (PLS) models based on full-spectral information, multiple linear regression (MLR) models and support vector machine (SVM) regression models based on the eight selected wavebands for soil TN content were established separately. After the comparison, the MLR and SVM models achieved higher accuracies than the PLS models based on the full spectral information. In addition, the SVM models got the best results. In the calibration group, the coefficients of determination ($R^2$) was 0.989, and the root mean square errors (RMSE) of calibration was 0.078 g/kg. In the validation group, the $R^2$ was 0.96, and the RMSE of prediction was 0.219 g/kg. The residual predictive deviation (RPD) was 5.426. For the soil samples with TN content in the range of 0–1 g/kg, the detection precision also reached a high level. Therefore, the eight sensitive wavebands selected through the ACO-MI method performed good mechanism, universality and predictive ability in soil TN content estimation. The ACO-MI method would be valuable for soil sensing in precision agriculture.

1. Introduction

Soil is the primary support for soil-grown crops. It is an important medium for plant root extension and the main nutrient source for crop growing. The main soil nutrients include TN, OM, available potassium, and available phosphorus (Chacón Iznaga et al., 2014; Sinfield et al., 2010). Among those soil nutrients, soil nitrogen (TN and available nitrogen) plays the most important role in promoting the growth of leaf, root, and stem and is a decisive factor to the crop yield (Bansod and Thakre, 2014). Excessive nitrogenous fertilization however will cause environmental pollution and crop distortion of growth and quality. The amount of nitrogen fertilizer applied therefore needs to be precisely controlled to ensure the crop yield and environmental protection. The fundament of precision fertilizing is effectively acquiring the soil information in the field. Rapid and precise acquisition of soil nitrogenous information in farmlands hence becomes increasingly important. The conventional method of detecting soil nitrogen content usually takes several days and consumes toxic chemicals. The conventional method

Abbreviations: TN, total nitrogen; OM, organic matter; NIR, near-infrared; MI, mutual information; ACO, ant colony optimization; PLS, partial least squares; MLR, multiple linear regression; SVM, support vector machine; $R^2$, coefficients of determination; SSR, sum of squares for regression; SST, sum of squares for total; SSE, sum of squares for error; RMSE, root mean square errors; RPD, residual predictive deviation

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also has several disadvantages, such as high requirements for detection personnel, expensive testing equipment, low efficiency, and environmental pollution (Debaene et al., 2014; Florinsky et al., 2002; Kuang and Mouazen, 2013; Moore et al., 1993; Nocita et al., 2014). By contrast, spectral analysis techniques are based on the internal relations between radiation energy and the composition and structure of matters. According to the characteristic spectra of matter, the target concentration or properties can be determined rapidly without chemicals (Igne et al., 2010; Vohland et al., 2011). For soil, the spectral information related to most of the organic radical containing hydrogen was in the NIR region (Li, 2006). NIR spectroscopy is a rapid, non-destructive, and non-pollutant testing method that plays an growing important role in soil nutrition measurement and exhibits extraordinary development potential in applications of soil TN content detection (Chang et al., 2001; Lucà et al., 2017; Morellos et al., 2016).

In the detection of soil TN content with NIR spectroscopy, the spectra of soil samples are first measured, and the NIR spectral data are then used as the input variables to establish the prediction models. Modern spectrometers possess high spectral resolution, and spectral data measurement generally involves hundreds or thousands of wavelength variables. Three kinds of information variables are involved in measurement of such super-large scale data. One is the effective informative variable, which can improve the model predictive ability because it reflects the characteristics of the target substance in the NIR region. The second is redundant or interfering variable, which is related with other targets. The last one is uninformative variable, which is irrelevant to the target material and usually caused by the measurement environment, such as noise. If the prediction model was established by the entire-spectrum information, then the latter two kinds of variables would increase the computation complexity and reduce the target prediction accuracy of the model. The multivariate calibration model is therefore a better choice when the informative variables could be selected appropriately, which can help in simplifying the calibration model and improving the model’s predictive ability in terms of accuracy, speed and robustness (Petrooulos et al., 2012; Sorol et al., 2010). Several studies confirmed that the models adopting limited characteristic wavebands only are better than the ones with entire-spectrum information. Cai et al. (2008) employed Monte Carlo uninformative variable elimination method to extract the characteristic bands and then established a PLS model to predict the sugar content of tomato. The results showed that the prediction accuracy and robustness of the proposed model were all better than the model on the basis of the entire band. Gao et al. (2009) proposed a method combining screened contribution and SPA to select soil TN content-sensitive wavebands. The result of the established multivariable model was more precise than the result derived from PLS for the entire spectra. Several scientists took advantage of the specific wavelength of the light source to develop a soil spectral detection device and obtained good detection accuracy (An et al., 2014; Li et al., 2010). The results revealed that the use of limited wavelength of light source in detecting soil nutrients had reached a practical level. The existing characteristic wavelength selection algorithm however revealed that several drawbacks in soil TN prediction remained. The selected wavebands had a weak mechanism interpretation about soil TN, and the accuracies of the established models were relatively low. The methods for selecting the characteristic wavebands therefore need to be further explored for the study of NIR spectral technology on soil TN content detection.

ACO is an evolutionary algorithm used to simulate the natural foraging behavior of ant colonies and was introduced in the early 1990s (Colorni et al., 1991). The technique is based on updating the coordination mechanism of seeking the shortest path to achieve intelligent search and parametric optimization. The ACO algorithm has been extensively applied in feature selection because of its prominent advantages, such as information positive feedback, distributed computation, heuristic search, robustness, and easy to combine with other algorithms (Dorigo et al., 1996; Aghdam and Kabiri (2016) proposed an intrusion detection system with features optimally selected using ACO to improve the performance. Varma et al. (2016) also used fuzzy entropy-based heuristic for ACO to search for the global best smallest set of network traffic features for real-time intrusion detection data set. Selection of the optimal spectral characteristic variable is also a combinatorial optimization issue. The features, such as global, discrete, and probability selection of self-adaptive ACO, are applicable to spectroscopy analysis. Hou et al. (2016) applied ant colony clustering algorithm to detect Grapevine leafroll disease (GLD) spectral anomalies on four GLD-infected vineyards from multi-spectral images for precision disease management. The classification accuracies of Non-, GLD-, GLD2-, and GLD3-infected grapevines were 94.4%, 75%, 84.6%, and 83.3%, respectively. Guo et al. (2014) selected sensitive wavebands from apple NIR spectroscopy using ACO–PLS optimized algorithm based on the features of heuristic global search and the random selection mechanism of Monte Carlo roulette to predict soluble solid content. The prediction model obtained a good prediction performance for SSC with correlation coefficients of 0.970, and RMSE of prediction of Brix of 0.514. Allegrini and Olivieri (2011) employed the concept of cooperative pheromone accumulation, which is typical of ACO selection methods, and optimized PLS models using a pre-defined number of variables and employing a Monte Carlo approach to discard irrelevant sensors. Ke et al. (2008) proposed an ACO-based algorithm to deal with feature selection in rough set theory and compared its performance with the simulated annealing-, genetic algorithm-, and Tabu search-based algorithms. The results showed the proposed algorithm achieved better performance according to both the classification results and the number of features. Santana et al. (2010) found ACO performed better than genetic algorithm-based feature selection method for ensemble classifiers when the number of individual classifiers was small. Agrawal and Kaur (2018) compared ACO and Hybrid Particle Swarm Optimization in test case selection. The results indicated ACO outperforms Hybrid Particle Swarm Optimization in the calculating efficiency.

The studies discussed above used ACO to carry out feature selection in numerous areas. After the comparison between ACO and other heuristic algorithms, ACO performs more flexible and efficient. It is especially suitable for the relatively small-scale problems (Xue et al., 2016). In order to make further improvement on the performance of ACO, the information theory, as a supplementary, could explore more and deeper information from the variables themselves. When using ACO, few researchers however adopt information theory to improve the performance of ACO in feature selection. Several studies adopted the Monte Carlo roulette principle to select features, which is random and lack connection with the variable information (Allegrini and Olivieri, 2011; Guo et al., 2014). In this way, the selected features were mostly dependent only on the performance of ACO. Merging ACO and information theory could significantly benefit feature selection, especially when the training set is not big enough to represent the whole application space.

In the early 1990s, Battiti (1994) and Lewis (1992) introduced MI theory into variable selection research. The feature selection method based on MI has gained considerable attention after 20 years of development. MI is an excellent tool for quantitatively calculating the common information between two random variables. The MI theory has therefore been extensively applied as an effective indicator for investigating correlation. MI can also be used to measure the arbitrary dependencies between random variables, which makes it suitable for assessing the “information content” of features in complex tasks.

Filter methods are defined by a criterion $J$ based on MI, also referred to as a “relevance index” or “scoring” criterion, which is intended to imply the potentially predictive ability of the feature (Duch, 2006). Moreover, there is another widely accepted point that an useful and parsimonious set of features is considered individually relevant and should not be redundant with respect to each other, which means that the selected features should not be highly correlated (Brown et al., 2012). This heuristic has been adopted numerous times. Battiti (1994)
presented MI feature selection criterion. Peng et al. (2005) proposed max-relevance min-redundancy criterion. Cheng et al. (2011) proposed a conditional MI feature selection criterion by using an assumption to approximate the terms on the basis of joint MI. Vinh et al. (2016) systematically investigated the issues of employing high-order dependencies for MI-based feature selection based on “relevancy” and “redundancy” criteria.

The variable selection methods above are all based on the principle of maximizing “relevancy” between the independent variables and the dependent variables and minimizing the “redundancy” between the selected independent variables. However, from the information theory perspective, another goal of feature selection is to select a feature subset that can contain most or all information of the original data set. The feature subset has the strongest representative ability of the entire data set.

The studies summarized above thus show that an effective featured waveband selection method is strongly needed for soil TN content prediction. This paper aims to propose a modified ACO algorithm mixed with a new evaluation criterion of waveband selection based on MI theory. This criterion would comprehensively consider three factors that demonstrate the relationships between independent and dependent variables, representative spectral information of the entire spectra, and discrepancies between the selected wavebands. To ascertain the universality and predictive ability of the selected wavebands, the soil samples under different kinds of fertilizers and covering wide TN content range were collected to validate the soil TN content prediction model.

2. Materials and methods

2.1. Experiment

The experiments were conducted from November 2014 to August 2016. Three experimental farms located in two representative areas of China, North China plain, and Northeast China plain were selected for this study, as shown in Fig. 1.

In November 2014, the experiments were conducted in Shangzhuang experimental farm (116.191794°E, 40.144091°N) of the China Agricultural University located in the North China plain. The soil type is sandy loam. A total of 270 sampling spots were selected randomly to collect soil samples. These samples were used to explore the sensitive wavebands of soil TN.

To validate the TN predictive ability and universality of the selected wavebands, two validation experiments were designed as described below.

The first validation experiment was also conducted in the Shangzhuang experimental farm in April 2015. Three different regions were selected with the distance of 50 m to avoid the interference from each other. Three kinds of fertilizers, namely, carbamide (N ≥ 27%), calcium nitrate (N ≥ 13%), and potassium nitrate (N ≥ 13.5%), were used separately to perform variable rate fertilization on the three regions mentioned above. Sixty soil samples (20 in each region) were collected, and the soil TN content of each sample was detected.

The second validation experiment was carried out in Heilongjiang Province in August 2016. Two farms located in the Northeast China plain, namely, Hongwei Farm and Shengli Farm, were selected. Hongwei farm (133.4472’E, 47.3125’N) covers 63,000 hm², and the soil type is meadow albic bleached soil. One hundred soil samples were collected in this farm. Shengli farm covers 87,733.33 hm², and two sampling areas were selected. The soil type in Shengli-A area (133.7247’E, 47.5277’N) is tufy soil, and the soil type in Shengli-B area (133.7530’E, 47.4044’N) is black soil. One hundred soil samples were collected in each part.

Finally, 630 samples were obtained and used as the target materials for all the subsequent experiments (NIR absorbance spectra measurement and soil TN detection).

2.2. Spectra measurement

All the soil samples were air dried, and the NIR spectroscopy absorbance of each sample was measured in the laboratory by a MATRIX-I type of FT-NIR analyzer with a rotating sample pool (Bruker Optical Company, Germany). Approximately 15 g of each soil sample was placed into a quartz cuvette with 48 mm diameter, and the cuvette was then placed into the rotating sample pool. The NIR spectra were finally measured by using the spectrometer. The spectral measurement range was 12,493–3899 cm⁻¹ (800–2564 nm) with resolution of 4 cm⁻¹ and scan times of 32. Each sample was scanned 10 times with three replications, and the mean value was considered the relative absorbance.

2.3. Measurement of soil TN content

After air drying, grinding, and sieving, the TN concentrations of soil samples were measured with a Kjeltc TM2300 azotometer (FOSS, Sweden). Air-drying soil powder amounting to 2.0 g was mixed with 6.2 g of K₂SO₄/CuSO₄·5H₂O catalyst (30:1), 20 ml of H₂SO₄ was then placed into the mixture, and the digestion was conducted at 420 °C for 1.5 h. The azotometer was finally used to distill cooling liquid and display nitrogen concentrations.

2.4. Data processing method

2.4.1. MI

MI is a key concept of information theory and used as a quantitative index of the correlation between two variables. This concept is also a quantitative index of the amount of information in one variable as that contained by the other variables. The MI theory can effectively eliminate the irrelevant information to the target components (y) from the spectral information (x). If x and y are continuous random variables with the existence of joint density μ(x,y) and edge density (μ_i(x), μ_j(y)), then MI can be defined as in Eq. (1).

\[ MI(x,y) = \sum_{x} \sum_{y} p(x,y) \log \frac{p(x,y)}{p(x)p(y)} \]  (1)

In Eq. (1), x and y represent two variables. MI(x,y) is the MI between x and y, which expresses the reductive amount of uncertainty of y after obtaining the information of x. Compared with other correlation analysis methods, MI can consider both linear and nonlinear relationship between variables.

A nonlinear relationship is ubiquitous among spectral information and between spectral response and material concentration (Benoudjit et al., 2004; Hu et al., 2011; Viscarrea Rossel et al., 2006). In this research, three MI-related indexes were calculated using Eq. (1). The first index is the MI values (MI(f; e)) between the soil absorbance (f) in the range of 800–2564 nm and TN content (c). The second index is the sum of all MI values (MI(f; s)) between the absorbance (ff(f ∈ F)) and the other absorbance (ff(f ∈ F – f)). F is the set of all wavelength absorbance. The third index is the sum of MI values (MI(f; s)) between the absorbance (ff(f ∈ F)) and the selected ones (ss(s ∈ S)). S is a set of selected wavelengths.

2.4.2. ACO

Combining the characteristics of ACO algorithm and the evaluation criteria for selecting feature variables proposed in this research, the modified algorithm called ACO-MI is shown as Eqs. (2)–(3) for the soil TN content-sensitive wavelength selection.

The probability of the kth ant to move from one wavelength to another can be described as Eq. (2).

\[ P_{ij}^{(k)}(t) = \alpha \times \tau_{ij}(t) + \beta \times \eta_{ij}(t) \]

\[ \eta_{ij} = \frac{1}{MI(f; s)} \]  (2)

Where \( P_{ij}^{(k)}(t) \) is the probability of the kth ant to move from wavelength \( f_i \) to wavelength \( f_j \) at time \( t \), \( \tau_{ij}(t) \) is the pheromone concentration from wavelength \( f_i \) to wavelength \( f_j \) at time \( t \), \( \alpha \) and \( \beta \) are constants, \( \eta_{ij} \) is the heuristic information from wavelength \( f_i \) to wavelength \( f_j \) at time \( t \), and \( MI(f; s) \) is the MI value between the absorbance at wavelength \( f \) and the selected one at wavelength \( s \).
In Eq. (2), $\tau_{ij}(t)$ represents the pheromone concentration between the wavelength $i$ and the wavelength $j$ at time $t$. $\eta_{ij}(t)$ represents the intensity of heuristic information, whose value indicates the divergence degree between wavelength $i$ where the ants are and the objective wavelength $j$. $\alpha$ and $\beta$ are the parameters that characterize the importance of pheromone concentration and heuristic factors. The greater the probability is, the greater the ants’ attractiveness is.

Eq. (2) demonstrates that ants mainly rely on two factors in selecting wavelength, pheromone concentration $\tau_{ij}(t)$, and heuristic information $\eta_{ij}(t)$. The value of $\eta_{ij}(t)$ does not change with time and the iterative updating rules of pheromone concentration because it is only related to the location of ants. Pheromone concentration $\tau_{ij}(t)$ thus also plays a major role in optimizing the global searching ability. After the ant completes a search of the characteristic variable, the pheromone is updated according to Eq. (3).

$$\tau_{ij}(t + 1) = (1 - \rho)\tau_{ij}(t) + \Delta\tau_{ij}(t)$$

$$\Delta\tau_{ij}(t) = Q \times L_k$$

$$L_k = \text{Norm}_{i,j}^2(\text{MI}(f; e)) + \text{Norm}_{i,j}^2\left(\sum_{j=1}^n \text{MI}(f; f_j)\right)$$

In Eq. (3), $\rho \in (0, 1)$ is the factor of evaporation that represents the disappearance speed of the pheromone. The selection of the value will affect the convergence speed of the algorithm. $\Delta\tau_{ij}(t)$ is the new pheromone concentration and is updated on the basis of the objective function and pheromone intensity factor. $Q$ is the new pheromone intensity factor used to adjust the objective function and the convergence rate. $L_k$ is the objective function. In this study, $L_k$ represents the sum of relevance degree with the target material (TN) and the total representative capacity for the entire-spectrum information of the selected wavelength by the current ant. The maximum of $L_k$ was then obtained to update the pheromone concentration.

### 2.5. Model accuracy evaluation methodology

The model accuracy was quantitatively evaluated with three aspects: $R^2$ calculated from Eq. (4), RMSE based on Eq. (5), and RPD calculated from Eq. (6) (Chakraborty et al., 2017; Mcgladdery et al., 2018; Williams, 1987).

$$R^2 = \frac{\text{SSR}}{\text{SST}} = 1 - \frac{\text{SSE}}{\text{SST}} = \frac{\sum^n_{i=1} (y_i - \bar{y})^2}{\sum^n_{i=1} (y_i - \bar{y})^2}$$

$$\text{SSR} = \sum^n_{i=1} (\hat{y}_i - \bar{y})^2; \text{SSE} = \sum^n_{i=1} (y_i - \hat{y}_i)^2$$

$$\text{SST} = \text{SSR} + \text{SSE} = \sum^n_{i=1} (y_i - \bar{y})^2$$

$$\text{RMSE} = \sqrt{\frac{\sum^n_{i=1} (y_i - \hat{y}_i)^2}{n}}$$

$$\text{RPD} = \sqrt{\frac{1/(n-1) \sum^n_{i=1} (y_i - \bar{y})^2}{1/n \sum^n_{i=1} (y_i - \bar{y})^2}}$$

where, $n$ indicates the number of samples, $y_i$ is the measured value of sample $i$, $\hat{y}_i$ is the predicted value of sample $i$, and $\bar{y}$ are the mean values of $y_i$.

### 3. Results and discussion

#### 3.1. Characteristic analysis of the original VIS/NIR spectra

All spectral curves of the soil samples were obtained by using the
spectrometer. Fig. 2 shows the spectral characteristic in the range of 800–2564 nm of the 36th soil sample and the 88th soil sample. The TN contents of the two samples were 0.684 and 0.884 g/kg, respectively. Fig. 2 reveals that the variation tendency of the soil spectral absorbance of the two samples becomes similar with each other with the change of soil TN content. In 800–930 nm, the spectral curve contained a considerable amount of noise because of the vibration of the measurement system. A slow downward trend was observed in the range of 930–1380 nm. An absorbance peak was observed in the range of 1380–1510 nm, which was caused by water absorbance. The soil spectral absorbance was then regained smoothly and steadily until 1850 nm. The soil spectral absorbance then sharply increased and reached its topmost peak at 1940 nm. A curve peak existed at around 2210 nm, which was different with the peaks around 1450 and 1940 nm in peak amplitudes. Viscarra Rossel et al. (2006) revealed that this spectral absorption band at around 2210 nm depended on the $O-H$ molecule. Most of the bound water is still in the soil samples and absorbs the light at the wavelengths of 1450 and 1940 nm in peak amplitudes. Viscarra Rossel et al. (2006) revealed that this spectral absorption band at around 2210 nm depended on the $O-H$ group of soil organic compounds.

Although the measured soil samples were air-dried, the absorption peaks were still evident near the wavebands of 1450 and 1940 nm, which were the absorption bands of the $O-H$ functional group in water molecule. Most of the bound water is still in the soil samples and absorbs the light at the wavelengths of 1450 and 1940 nm because the air-dried treatment can only remove free water (Li, 2006).

### 3.2. Sensitive waveband selection based on MI

As mentioned above, this paper aimed to propose a novel evaluation criteria for selecting feature variables and then develop a method according to MI theory based on the criteria. Three kinds of relationships were considered. The variable selection method focuses on maximizing MI between the candidate spectral variable and the target material (TN), minimizing the redundancy between the candidate and the selected spectral variables, and maximizing the ability of the candidate variables representing for the entire-spectrum variables. Based on the above principles, this study developed a general expression formula shown as Eq. (7).

$$y = \text{Norm}_1(\text{MI}(f_i;c)) + \text{Norm}_2\left(\sum_{j=1}^{n} \text{MI}(f_i;f_j)\right) - \text{Norm}_3\left(\sum_{k=1}^{n} \text{MI}(f_k;S)\right)$$

(7)

where $F$ is the set of absorbance of candidate wavebands, and $i \in F$. $K$ is the set of absorbance of all wavebands, $f \in K$. $S$ is the set of selected wavebands, $k \in S$. $c$ is the dataset of soil TN contents. $n$ is the number of all wavelengths. $m$ is the number of selected wavelengths.

The process of the feature selection is expressed as follows:

1) Initialization. $F$ and $K$ are sets of absorbance of all wavebands. $S$ is a null set.

2) Computing $\text{MI}(f_i;c)$ and $\sum_{j=1}^{n} \text{MI}(f_i;f_j)$, and then conducting normalization processing in the range of 0–1 between the two indexes.

3) Selecting the first sensitive waveband $i_1$ to make the sum of $\text{Norm}_1(\text{MI}(f_i;c))$ and $\text{Norm}_2\left(\sum_{j=1}^{n} \text{MI}(f_i;f_j)\right)$ be the maximum, and then $F = F - i_1$, $S = i_1$.

4) Calculating $\text{MI}(f_i;c)$, $\sum_{j=1}^{n} \text{MI}(f_i;f_j)$, and $\sum_{k \in S} \text{MI}(f_k;S)$, and then performing normalization processing among the three indexes.

5) The wavelength $f_i$ was used as the next sensitive wavebands, which could make the result of Eq. (7) be maximum, and $F = F - f_i$, $S = S \cup f_i$.

6) Until the number of the selected wavelength reaches the maximum, the sensitive wavelength selection ends, or it will move to Step 4.

As for the maximum number of needed wavelengths, if the number is small, the selected wavelength could not represent the effective spectral information comprehensively. Meanwhile, considering a future possibility of constructing a multispectral device for soil TN content detection, large number of selected wavelength would increase cost and the complexity of structure. According to the prior trials (An et al., 2014; Zhang et al., 2016; Zhang et al., 2015), the maximum of the needed variables in this research is set as eight.

Fig. 3 shows two normalizing MI curves. “MI-c” represents the MI between the absorbance and the TN content, which could indicate the correlation degree of the waveband and TN content. Every point on “MI-wav” represents the sum of MI values between the absorbance at this wavelength and each absorbance of all other wavebands. This curve could represent the ability of different wavebands representing full spectral information. Fig. 3 shows that the MI value between the absorbance and TN fluctuated significantly at the beginning around 800–900 nm, because the spectral curve contained a considerable amount of noise. Numerous local maximum points were observed afterward. MI can express more spectral information of soil TN than the regular linear correlation curve because it contains linear and non-linear relationships between each spectral variable and TN content. The
Fig. 4. Featured waveband selection processes.
absorbance at 1895 nm possessed the strongest ability to represent full spectral information.

On the basis of the principles of this selection method, eight sensitive wavebands were selected individually as shown in Fig. 4. In the first selection, 1895 nm was the maximum in the curve, which represents the sum of MI-c and MI-wav. Therefore, 1895 nm was the first selected sensitive waveband. In the second selection, 980 nm was the maximum of the curve, which were calculated as Eq. (7). The same procedure was repeated for the next selections. The first eight selection processes were shown in Fig. 4. Then 1895, 980, 1323, 839, 2284, 978, 1767, and 972 were determined individually as the sensitive wavebands of soil TN content. From the entire featured waveband selection, the MI characteristic curves in the second, sixth, and eighth selection were almost in the similar trend, which lead to the selected wavebands (972, 978, and 980 nm) in these processes to be all approximately 980 nm, which implied that several selected featured bands were in the narrow range with high self-correlation and redundancy. Moreover, 980 nm is related to the O–H groups’ stretching vibration from water absorption (Leiva-Valenzuela et al., 2013; Pan et al., 2016). A typical large absorption band is observed in the range of 960–980 nm for the second O–H water overtone (Helgerud et al., 2012). A strong absorption features was centered at 1900 nm which is related to O–H molecules (Demattê et al., 2004). Therefore, using MI method alone for sensitive wavelength selection could not effectively reduce the redundancy among the selected feature wavelengths nor eliminate the interference from soil water. Further research on soil TN content-sensitive waveband selection is needed.

3.3. Sensitive waveband selection based on the ACO–MI method

Considering the outstanding advantages of ACO in feature selection, this research combined ACO and the evaluation criteria based on MI to optimize the results of soil TN content-sensitive waveband selection. The maximum variable number was also set to 8. The flow chart of the entire process of sensitive waveband selection based on ACO is shown in Fig. 5.

1) Initialization. The parameters of ACO algorithm were set after multiple experimental verifications. The maximum iteration time was 3; the ant colony size was 1500; the importance degrees of heuristic factor and pheromone were 0.8 and 0.2, respectively; the evaporation factor was 0.5; and the pheromone intensity factor was 0.0003.

2) Calculate the MI(f_i;c) of all wavelengths, and create an n × n matrix of MI(f_i,f_j).

3) All the initial pheromone vector values were set to be 1, which implied that each wavelength had the same attractiveness to the ants.

4) Place ants on n wavelengths and activate the ants to select the featured variable based on the probability function shown as Eq. (2).

5) Calculate the objective function using Eq. (3), which indicates the entire-spectrum representative ability and the relevance with the soil TN content of the selected wavelengths, and then update the pheromone. If the number of selected variables does not reach its set maximum, then it will move to Step 4, or it will move to the succeeding step.

6) Evaluate the iteration time to determine whether the set maximum is reached or not. If the set maximum is not reached, then the pheromone would be set as 1, and process is repeated starting with Step 3, or it would go to the succeeding step.

7) Compare the objective function results after all iterations and identify the group of selected wavebands with high objective function result as the sensitive wavebands to soil TN content.

After the selection shown in the flow chart (Fig. 5), eight wave-lengths of 943, 1004, 1097, 1351, 1550, 1710, 2123, and 2254 nm were
determined as the sensitive wavebands. As shown in Fig. 6, the selected wavelengths were distributed in the entire spectral curve. The integration of ACO and the selection criteria of sensitive wavebands based on MI could therefore effectively avoid repeated selection in a narrow waveband and eliminate the interference from soil moisture compared with the method of adopting MI technology only.

The previous study revealed that the wavelength of approximately 940 nm was sensitive to soil OM, which was identified by stepwise MLR and PLS (Kweon and Maxton, 2013). Palacios-Orueta and Ustin (1998) found that the area of approximately 1000 nm was related to Fe and OM content in soil. The reflectance at wavelength 1100 nm was also the OM estimators (Daniel et al., 2004). Sun et al. (2009) selected 1350 nm as one of the sensitive wavelengths of soil OM according to the correlation analysis. TN is widely known to have a strong relationship with OM content in soil, because N is a major component of OM. Among the eight selected wavelengths, An et al. (2014) and Bansod and Thakare (2014) adopted three wavelengths, namely, 940, 1100, and 1550 nm, to develop portable soil nitrogen detectors. Both detectors are reliable in soil nitrogen content measurement. Aside from 1000 nm, 1710 nm was also related to Fe. A curvilinear relationship between Fe₂O₃ and the reflectance at 1710 nm produces a large squared correlation coefficient (r = −0.91 or r² = 0.85) (Galvão et al., 2001). Fe could help fertilizer N transfer into available N in soil (Ali et al., 1998). In addition, 2120 and 2250 nm were crucial for TN estimation based on the correlation analysis of differential spectral information (Shi et al., 2013; Zhang et al., 2014).

All the eight wavelengths selected through the modified ACO algorithm therefore had direct and close relationship with soil TN content, which verified the effectiveness of the ACO–MI method in wavelength selection of soil TN content. The ACO–MI method also successfully eliminated the interference from the soil moisture, which was critical to TN content-sensitive wavelength selection.

3.4. Soil TN content modeling and validation

To further verify the TN predictive ability and universality of the selected sensitive wavelengths, this study created a mixed dataset containing the soil samples collected from different regions (i.e., North China plain and Northeast China plain), in different soil types, including sandy loam, meadow albic bleached soil, turfy soil, and black soil. All the spectral curves were checked prior to the modeling. Three samples were lost in the field experiment, and the spectral information of one sample collected from Northeast China plain was abnormal, which may have been caused by misoperation in the spectra measurement. A total of 626 soil samples were thus used to establish the prediction model. The TN contents of 626 soil samples in the mixed dataset were in the range of 0.061–2.743 g/kg. The PLS models based on full-spectral information, MLR and SVM regression models based on the eight selected wavelengths for soil TN content were established separately. Samples were divided into two groups, as is, 450 were the under calibration group and the remaining 176 samples were under the validation group. The input data of PLS models were the absorbance of soil samples in the range of 800–2564 nm. The MLR model was established as Eq. (8).

\[
y = -1.9 + 9.23x_{04} - 1.44x_{004} - 19.15x_{097} - 38.93x_{351} + 183.37x_{150} - 119.59x_{170} + 1.44x_{332} - 10.18x_{0254}
\]

where \( y \) is the TN content of the soil samples, and \( x_i \) is the absorbance value of wavelength \( i \).

According to the established model, the 1:1 relationship diagrams were drawn between the prediction and observation to demonstrate the reliability and consistency of the selected model. The results are shown in Figs. 7–9.

The accuracies of the three models are shown in Table 1. Both of the two models established by the selected wavelengths obtained higher overall predictive abilities than the one based on the full spectral information. While for the MLR model, five soil samples in the whole dataset (626 points) were predicted to be negative values. The TN contents of the five points were in the range of 0.1–0.2 g/kg. It indicated that the MLR model has a limitation in predicting soil TN with a low content. For the SVM model, the accuracies of the calibration and validation were increased significantly. And the drawbacks of predicted negative values of TN contents of MLR model were mended. While for the three models, when the soil samples with TN content around 2 g/kg, some prediction TN values were higher than the measured values. These soil samples mainly belonged to turfy soil and contained a high amount of plant debris, humus, and several minerals, which were not thoroughly broken down. The prediction TN values using spectral information, including the TN in soil and a part of TN in the
undecomposed materials in soil, were thus higher than the measured TN values. The values would be closer if the soil samples’ spectra were collected after grinding and sieving.

The TN contents of 528 soil samples were in the range of 0–1 g/kg, which were the major part of all soil samples. Moreover, the majority of soil in cultivated land were in this nutritional level. The PLS, MLR and SVM models were therefore established among this part. The 378 samples were used for calibration and the remaining 150 samples were for validation. The MLR regression model was established as Eq. (9).

The optimal penalty $C$ and the optimal kernel function $g$ of the SVM regression models were 512 and 0.25 after the optimization.

\[
y = -0.53 - 2.42x_{463} - 2.47x_{504} + 12.49x_{547} - 12.99x_{155} + 28.99x_{159} \\
- 20.39x_{710} + 5.54x_{216} - 6.64x_{254}
\]  

(9)

Where $y$ is the TN content of the soil samples, and $x_i$ is the absorbance value of wavelength $i$.

The results of the three models were highlighted in Figs. 10–12.

Table 1: Accuracies of PLS, MLR and SVM models.

<table>
<thead>
<tr>
<th></th>
<th>PLS</th>
<th>MLR</th>
<th>SVM</th>
</tr>
</thead>
<tbody>
<tr>
<td>Calibration R^2</td>
<td>0.901</td>
<td>0.96</td>
<td>0.986</td>
</tr>
<tr>
<td>RMSE of calibration (g/kg)</td>
<td>0.238</td>
<td>0.153</td>
<td>0.078</td>
</tr>
<tr>
<td>Validation R^2</td>
<td>0.92</td>
<td>0.94</td>
<td>0.96</td>
</tr>
<tr>
<td>RMSE of prediction (g/kg)</td>
<td>0.224</td>
<td>0.168</td>
<td>0.219</td>
</tr>
<tr>
<td>RPD</td>
<td>5.198</td>
<td>7.253</td>
<td>5.426</td>
</tr>
</tbody>
</table>

The accuracies of the three models are shown in Table 2. No matter for the linear regression model (MLR) or the non-linear regression model (SVM), the predicting accuracies of soil TN contents in this range all got better results than the PLS model, which demonstrated that the selected eight sensitive wavebands could represent the full spectral information effectively, and predict the TN, especially in farmland soil, stability, universality, and veracity.

The verification of the samples under four soil types collected from different farms revealed that although the eight sensitive wavelengths were selected from 270 original soil samples collected from a specific region with a single type, the wavelengths still performed with higher universality and predictive ability than the full spectrum in TN content detection of different soil types. The eight selected sensitive wavebands had close mechanism correlation with the material of TN.

3.5. Discussion

Prior work has documented the advantages of soil nutrients estimation using limited wavelengths. However, the selected wavelengths had a weak mechanism interpretation about soil TN, which might lead to the lack of universality and predictive ability of the established models. In this study, we put forward a novel method based on ACO and MI to select the sensitive wavebands of soil TN content and verified universality and estimation ability of the selected wavelengths from the aspects of mechanism, model types and sample’s composition.
The comparison among full spectral PLS models, Linear (MLR) and non-linear (SVM) regression models.

Table 2

<table>
<thead>
<tr>
<th></th>
<th>PLS</th>
<th>MLR</th>
<th>SVM</th>
</tr>
</thead>
<tbody>
<tr>
<td>Calibration R²</td>
<td>0.748</td>
<td>0.872</td>
<td>0.922</td>
</tr>
<tr>
<td>RMSE of calibration (g/kg)</td>
<td>0.136</td>
<td>0.087</td>
<td>0.069</td>
</tr>
<tr>
<td>Validation R²</td>
<td>0.721</td>
<td>0.841</td>
<td>0.871</td>
</tr>
<tr>
<td>RMSE of prediction (g/kg)</td>
<td>0.145</td>
<td>0.1</td>
<td>0.099</td>
</tr>
<tr>
<td>RPD</td>
<td>2.626</td>
<td>3.896</td>
<td>3.864</td>
</tr>
</tbody>
</table>

Note: Nsample is the number of samples; $R^2$ is validation $R^2$.

In light of the fact that for different TN ranges, there may exist optimal estimation models with best accuracies, a further accuracy improvement can be achieved by training at multiple range steps and develop an automatic range-model selection instrument.

Given the recent advances in deep learning, another effort can be invested by employing a separate part in the model for adaptation of computing SVM model based on the “interrelations merit model” of the eight bands. That is the SVM computing (or visible layer) may be affected by another hidden layer that was trained to estimate the “relevance” of each band to the other seven and adapt the SVM parameters accordingly. In that way, some small or even large “noisy” influence on one or several bands (i.e. by water content or OM or other influential constituents) could be eliminated or reduced, or even auto band reject, and thus increase the accuracy of the estimate.

The research provide an innovative and flexible spectral feature extraction method, which could be also applied into other areas. The results of this study are significant for the processing of hyperspectral information and the development of multi-spectral sensors in the future.

4. Conclusions

To effectively extract the sensitive wavebands of soil TN content, a selection criterion based on MI and ACO methods was innovatively proposed to screen the sensitive wavebands of soil TN content. The obtained bands were then used to predict the TN content in the soil samples, which were collected from different farms and under four soil types, also including the samples under different fertilization conditions, to verify the universality and predictive ability. The main conclusions are as follows:

(1) After wavelength selection using ACO-MI method, 943, 1004, 1097, 1351, 1550, 1710, 2123, and 2254 nm were determined as soil TN content-sensitive wavebands. According to the mechanism analysis, all the eight wavelengths had direct and close relationship with TN content-sensitive wavebands selected using ACO-MI method in this research were dramatically larger than the rest, which would all lead to relatively low accuracies. This research further verify the universality and predictive ability of the sensitive wavelength in predicting soil TN content.

Acknowledgments

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