

Author's Accepted Manuscript

Public debt, discretionary policy, and inflation persistence

Stefan Niemann, Paul Pichler, Gerhard Sorger



www.elsevier.com/locate/jedc

PII: S0165-1889(13)00025-0

DOI: <http://dx.doi.org/10.1016/j.jedc.2013.01.014>

Reference: DYNCON2795

To appear in: *Journal of Economic Dynamics & Control*

Received date: 12 September 2011

Revised date: 19 June 2012

Accepted date: 23 January 2013

Cite this article as: Stefan Niemann, Paul Pichler and Gerhard Sorger, Public debt, discretionary policy, and inflation persistence, *Journal of Economic Dynamics & Control*, <http://dx.doi.org/10.1016/j.jedc.2013.01.014>

This is a PDF file of an unedited manuscript that has been accepted for publication. As a service to our customers we are providing this early version of the manuscript. The manuscript will undergo copyediting, typesetting, and review of the resulting galley proof before it is published in its final citable form. Please note that during the production process errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.

Public debt, discretionary policy, and inflation persistence

Stefan NIEMANN* Paul PICHLER† Gerhard SORGER‡

February 13, 2013

Abstract

We describe a simple mechanism that generates inflation persistence in a standard sticky-price model of optimal fiscal and monetary policy. Key to this mechanism is that policies are implemented under discretion. The government's discretionary incentive to erode the real value of nominal public debt by means of surprise inflation renders inflation expectations and, in further consequence, equilibrium inflation rates highly correlated with the stock of public debt. Debt, in turn, is highly persistent, allowing for tax-smoothing in the face of disturbances. Due to the aforementioned correlation, the persistence in debt carries over to inflation. Our analysis uncovers a non-monotonic effect of nominal rigidities on inflation persistence and shows that government debt under discretion does *not* display the near random walk property familiar from the Ramsey literature. A calibrated version of the model that incorporates a moderate degree of monopolistic competition and price stickiness is quantitatively consistent with the inflation dynamics experienced in the U.S. since the Volcker disinflation of the early 1980s.

JEL classification: E52, E61, E63

Keywords: Inflation dynamics; persistence; optimal fiscal and monetary policy; lack of commitment

*Department of Economics, University of Essex, United Kingdom. E-mail: sniem@essex.ac.uk

†Corresponding author. Economic Studies Division, Oesterreichische Nationalbank, Austria. E-mail: paul.pichler@oenb.at

‡Department of Economics, University of Vienna, Austria. E-mail: gerhard.sorger@univie.ac.at

1 Introduction

Ramsey models of optimal fiscal and monetary policy typically predict inflation rates that are negative on average and display almost zero persistence (Chari, Christiano, and Kehoe, 1991; Khan, King, and Wolman, 2003; Schmitt-Grohe and Uribe, 2004, 2010; Siu, 2004). This empirically implausible prediction has recently been stressed by Chugh (2007), who shows that an otherwise standard model augmented with habits-in-consumption and physical capital accumulation can generate substantial inflation persistence under Ramsey policies. In his model, an increased preference or ability to smooth consumption over time leads to a highly persistent real interest rate; a persistent real interest rate, in turn, implies a persistent inflation rate by the Fisher relationship.

The present paper describes an alternative mechanism that generates realistic inflation persistence. We study a fairly standard sticky-price model and argue that optimal inflation rates are highly persistent if policies are implemented under discretion rather than commitment. Key to this result is the government's discretionary incentive to erode the real value of outstanding liabilities by means of surprise inflation. This incentive renders inflation expectations and, in further consequence, equilibrium inflation rates correlated with the level of outstanding debt. Since optimal policies use public debt as a means to smooth tax distortions over time, it displays a high degree of persistence. Due to the aforementioned correlation, this persistence carries over to inflation.

Nominal rigidities affect optimal inflation persistence in a non-monotonic way, as two opposing effects are at work. On the one hand, the correlation between debt and inflation becomes weaker as price variations become more costly. On the other hand, the persistence of debt under optimal policies increases in the presence of nominal rigidities: When price adjustments are costly, the policy-maker refrains from using inflation as a shock absorber but uses persistent changes in debt to smooth the effects of shocks over time. Whether an increase in price stickiness raises or lowers inflation persistence therefore depends on which of the two effects is stronger. For a calibrated economy, we show that at very low levels of price stickiness the *reduced correlation effect* dominates, such that inflation persistence decreases in the amount of price stickiness. At higher levels of price stickiness, the *debt persistence effect* dominates and inflation persistence accordingly increases. The inflation dynamics generated from our calibrated economy are quantitatively consistent with empirical data for the U.S. since the Volcker disinflation.

Our results also indicate that the dynamic properties of debt under optimal discretionary policy are qualitatively different from those under commitment. Under commitment, debt is used by the government to smooth the distortionary effects of shocks over time and displays a near-random walk property, i.e., temporary innovations to the public budget are financed

by permanent changes in taxes and debt (Schmitt-Grohe and Uribe, 2004). Under discretion, variations in the stock of debt in response to adverse shocks are costly, as they induce increased inflation expectations. These, in turn, lead to higher realized inflation rates in equilibrium and therefore higher price adjustment costs and higher nominal interest rate distortions. In light of these costs, the government optimally decides to keep debt in close vicinity of its steady state level. Importantly, this implies that unlike in the Ramsey framework temporary innovations in the public budget are *not* financed by permanent changes in taxes and debt, i.e., the near-random walk behavior of taxes and debt observed under commitment is overturned under discretion.

The remainder of this paper is organized as follows. Section 2 lays out the model economy and characterizes the private-sector equilibrium for given policies. Section 3 presents the optimal policy problem. Section 4 discusses the calibration and numerical solution of the model. Section 5 presents our main findings and confronts the model’s predictions regarding inflation dynamics with the empirical evidence in the U.S. since the Volcker disinflation of the early 1980s. Section 6 discusses the related literature, and Section 7 concludes.

2 The model

Similar to Schmitt-Grohe and Uribe (2004), we consider an infinite-horizon production economy populated by a large number (a continuum of measure one) of identical private agents and a government. The private agents act both as consumers and as producers; they operate under imperfect competition and set nominal prices subject to price adjustment costs. A demand for money arises due to its role in facilitating consumption transactions. Time evolves in discrete periods $t \in \{0, 1, 2, \dots\}$.

2.1 The private sector

The preferences of the representative private agent are defined over sequences of consumption, $(c_t)_{t=0}^\infty$, and labor effort, $(h_t)_{t=0}^\infty$, and are given by

$$E_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - \alpha h_t], \quad (1)$$

where E_0 denotes the mathematical expectation operator conditional on information available in period 0, $\beta \in (0, 1)$ is the time-preference factor, and $\alpha > 0$ is the constant marginal utility of leisure. We assume that the function u satisfies standard monotonicity, curvature and smoothness properties.

The agent enters period t holding M_t units of money and B_t units of one-period risk-free bonds issued by the government. Each of these bonds pays one unit of money when it matures at the end of period t . The agent has two sources of income in period t . First, it supplies h_t units of labor to a perfectly competitive labor market, earning the nominal after-tax wage income $(1 - \tau_t)W_t h_t$, where τ_t and W_t denote the tax rate and the nominal wage rate in period t . Second, it earns profits from producing a differentiated intermediate good, which forms an input for the production of the final consumption good. Each agent has access to a linear production technology $\tilde{y}_t = a_t \tilde{h}_t$, which takes labor \tilde{h}_t as the only input and is subject to a stochastic productivity a_t . Notice that, while h_t is the agent's own labor supply, \tilde{h}_t is the amount of labor it demands on the labor market to produce the intermediate good. Labor productivity a_t is the same for all agents and evolves according to

$$\log a_{t+1} = \rho_a \log a_t + \varepsilon_{t+1}^a,$$

where ρ_a measures the autocorrelation of labor productivity and $\varepsilon_{t+1}^a \sim N(0, \sigma_{\varepsilon^a}^2)$ denotes the period- $(t+1)$ innovation.

The final consumption good is a Dixit-Stiglitz aggregate of all intermediate goods. We denote by $\theta > 1$ the constant elasticity of substitution between any two intermediate inputs. When $\theta \rightarrow \infty$, the economy approaches the limiting case of perfectly competitive product markets. Denoting by \tilde{P}_t the price of an intermediate good charged by its monopolistic producer and by P_t the aggregate price level, the demand for the intermediate good depends on aggregate output y_t and the relative price \tilde{P}_t/P_t according to

$$d(\tilde{P}_t, P_t, y_t) = y_t \left(\frac{\tilde{P}_t}{P_t} \right)^{-\theta}.$$

When choosing its price \tilde{P}_t , the agent takes the demand function d together with the aggregate variables P_t and y_t as given. Finally, we assume that there are quadratic costs to price adjustment as in Rotemberg (1982), which in real terms amount to

$$\frac{\kappa}{2} \left(\frac{\tilde{P}_t}{\tilde{P}_{t-1}} - 1 \right)^2. \quad (2)$$

The parameter κ in (2) measures the size of price adjustment costs; when $\kappa = 0$ prices are flexible.

Finally, we follow Schmitt-Grohe and Uribe (2004) and postulate that each agent has to pay a proportional transaction cost $s(v_t)$ when purchasing c_t units of the consumption good. Here,

v_t is the agent's consumption-based money velocity defined by

$$v_t = P_t c_t / M_t. \quad (3)$$

Hence money is valued because it facilitates transactions. Notice that the timing assumption underlying the definition of velocity in (3) implies that agents cannot reduce their transaction costs by rearranging their nominal asset portfolios at the start of a period, but that they are bound by their predetermined money holdings M_t . Thus, the velocity-based transaction cost $s(v_t)$ reflects a timing assumption corresponding to the cash-in-advance setting in Svensson (1985).¹ As for the function s itself, we assume that (i) s takes non-negative values and is twice continuously differentiable with first and second derivative s_v and s_{vv} , (ii) there exists a satiation level $\underline{v} > 0$ such that $s(\underline{v}) = s_v(\underline{v}) = 0$, (iii) $(v - \underline{v})s_v(v) > 0$ for all $v \neq \underline{v}$, and (iv) $2s_v(v) + vs_{vv}(v) > 0$ for all $v \geq \underline{v}$. As discussed by Schmitt-Grohe and Uribe (2004), these assumptions guarantee that money demand is decreasing in the nominal interest rate and that the Friedman rule is not associated with an infinite money demand.

Finally, the agent's budget constraint in period t is given by

$$\begin{aligned} M_t + B_t + (1 - \tau_t)P_t w_t h_t + \tilde{P}_t y_t \left(\tilde{P}_t / P_t \right)^{-\theta} - P_t w_t \tilde{h}_t - (\kappa/2) \left(\tilde{P}_t / \tilde{P}_{t-1} - 1 \right)^2 P_t \\ \geq P_t c_t [1 + s(v_t)] + M_{t+1} + q_t B_{t+1}, \end{aligned} \quad (4)$$

where $w_t = W_t / P_t$ is the real wage, and q_t denotes the price of bonds purchased in period t , i.e., q_t is the inverse of the gross nominal interest rate on these bonds.

2.2 The government

The government is benevolent and decides over monetary and fiscal policy instruments. It faces a stream of exogenous, stochastic and unproductive expenditures $(g_t)_{t=0}^\infty$, which evolves according to

$$\log g_{t+1} = (1 - \rho_g) \log \bar{g} + \rho_g \log g_t + \varepsilon_{t+1}^g.$$

The parameter \bar{g} denotes the steady state level of government expenditures, ρ_g is the autocorrelation coefficient, and $\varepsilon_{t+1}^g \sim N(0, \sigma_{\varepsilon^g}^2)$. To finance its expenditures, the government imposes a proportional labor income tax at rate τ_t , issues government bonds \bar{B}_{t+1} , and receives seigniorage income $\bar{M}_{t+1} - \bar{M}_t$.² Monetary policy manages the supply of money \bar{M}_{t+1} and sets the price of

¹This timing protocol is essential within our model because it makes unanticipated inflation costly, which prevents the discretionary government from using surprise inflation as a non-distortionary source of revenues.

²Where necessary, we use bars to distinguish aggregate variables from their individual counterparts.

bonds q_t . The consolidated government budget constraint in nominal terms is thus given by

$$\tau_t P_t w_t h_t + (\bar{M}_{t+1} - \bar{M}_t) + q_t \bar{B}_{t+1} \geq P_t g_t + \bar{B}_t. \quad (5)$$

The policy instruments τ_t , \bar{B}_{t+1} , q_t , and \bar{M}_{t+1} must be chosen in such a way that (5) holds and that the markets for bonds and money clear.

2.3 Private-sector equilibrium

The individual household takes aggregate output, the wage rate, the price level, and the government's policies as given and maximizes lifetime utility subject to its budget constraint. The Lagrangian associated with this optimization problem reads

$$\begin{aligned} \mathcal{L}^H = E_0 \sum_{t=0}^{\infty} \beta^t & \left\{ u \left(\frac{v_t m_t}{1 + \pi_t} \right) - \alpha h_t + \lambda_t \left[\frac{m_t + b_t}{1 + \pi_t} + (1 - \tau_t) w_t h_t + y_t (\tilde{p}_t)^{1-\theta} \right. \right. \\ & \left. \left. - \frac{w_t}{a_t} y_t (\tilde{p}_t)^{-\theta} - \frac{\kappa}{2} \left(\frac{\tilde{p}_t}{\tilde{p}_{t-1}} (1 + \pi_t) - 1 \right)^2 - \frac{v_t m_t}{1 + \pi_t} [1 + s(v_t)] - m_{t+1} - q_t b_{t+1} \right] + \nu_t \left[c_t - \frac{v_t m_t}{1 + \pi_t} \right] \right\}. \end{aligned} \quad (6)$$

In the above representation we have eliminated the variable $\tilde{h}_t = y_t (\tilde{P}_t/P_t)^{-\theta}/a_t$, and we have introduced real money holdings $m_{t+1} = M_{t+1}/P_t$, real bond holdings $b_{t+1} = B_{t+1}/P_t$, the relative price $\tilde{p}_t = \tilde{P}_t/P_t$, and the net inflation rate $\pi_t = P_t/P_{t-1} - 1$. Finally, λ_t and ν_t denote Lagrangian multipliers.

The solution to the household's optimization problem is characterized by a set of standard first-order optimality conditions. Imposing on these conditions that all private agents are identical and that markets clear, i.e., $\bar{m}_t = m_t$, $\bar{b}_t = b_t$, $\tilde{p}_t = 1$, and $y_t = a_t h_t$, we obtain the following set of conditions that characterize a symmetric private-sector equilibrium for given government policies:

$$0 = c_t - \frac{v_t m_t}{1 + \pi_t}, \quad (7)$$

$$0 = u'(c_t) - \lambda_t [1 + s(v_t) + v_t s'(v_t)], \quad (8)$$

$$0 = -\alpha + \lambda_t (1 - \tau_t) w_t, \quad (9)$$

$$0 = w_t - \frac{\theta - 1}{\theta} a_t - \frac{\kappa}{\theta h_t} \pi_t (1 + \pi_t) + \beta \frac{\kappa}{\theta h_t} E_t \frac{\lambda_{t+1}}{\lambda_t} \pi_{t+1} (1 + \pi_{t+1}), \quad (10)$$

$$0 = -\lambda_t + \beta E_t \frac{\lambda_{t+1}}{1 + \pi_{t+1}} [1 + v_{t+1}^2 s'(v_{t+1})], \quad (11)$$

$$0 = -\lambda_t q_t + \beta E_t \frac{\lambda_{t+1}}{1 + \pi_{t+1}}. \quad (12)$$

The first three equations characterize the household's optimal choice of consumption, the consumption-based money velocity, and the labor supply. Equations (10)-(12) are, respectively, a purely forward-looking New Keynesian Phillips curve and the household's Euler equations for money and bonds.

Finally, notice that equations (7)-(9) and the aggregate resource constraint allow us to express the private-sector equilibrium realizations of c_t , λ_t , τ_t , and h_t as functions of other decision variables. Specifically,

$$c_t = \hat{c}(v_t, \pi_t, m_t) = v_t m_t / (1 + \pi_t), \quad (13)$$

$$\lambda_t = \hat{\lambda}(v_t, \pi_t, m_t) = u' \left(\frac{v_t m_t}{1 + \pi_t} \right) [1 + s(v_t) + v_t s'(v_t)]^{-1}, \quad (14)$$

$$\tau_t = \hat{\tau}(v_t, \pi_t, m_t, w_t) = 1 - \frac{\alpha}{w_t} \left[u' \left(\frac{v_t m_t}{1 + \pi_t} \right) \right]^{-1} [1 + s(v_t) + v_t s'(v_t)], \quad (15)$$

$$h_t = \hat{h}(v_t, \pi_t, m_t, a_t, g_t) = \frac{1}{a_t} \left[\left(\frac{v_t m_t}{1 + \pi_t} \right) [1 + s(v_t)] + g_t + \frac{\kappa}{2} \pi_t^2 \right]. \quad (16)$$

These functions will be useful to ease notation in the following section where we present the government's optimal policy problem.

3 The optimal policy problem

The government's objective is to maximize the lifetime utility (1) of the representative household subject to the private-sector equilibrium conditions and to decentralize the desired allocation via the appropriate choice of its policy instruments τ_t , q_t , b_{t+1} , and m_{t+1} .³ However, the government is subject to a well-known time-inconsistency problem: It would like to use surprise inflation as a means to erode the real value of its nominal debt burden, since this policy resembles a lump-sum tax on the private sector's financial wealth; moreover, monopolistic competition and nominal rigidities create incentives for using surprise inflation to raise output above its suboptimal equilibrium level. The Ramsey literature addresses this problem by assuming that the government can nevertheless commit to implement its (time-inconsistent) policy plans. In the present paper we depart from this assumption and study optimal policies implemented by a purely discretionary government.⁴

A convenient way to characterize optimal discretionary policies is to assume that the gov-

³Notice, however, that as a consequence of money and bond market clearing conditions the policy maker has only two degrees of freedom when choosing these variables.

⁴Recent contributions along these lines include Diaz-Gimenez, Giovannetti, Marimon, and Teles (2008), Martin (2009), and Niemann (2011), among others. However, these papers introduce money via a cash constraint and abstract from monopolistic competition and nominal rigidities.

ernment actually consists of an infinite sequence of separate policy-makers, one for each period. Each of these policy-makers seeks to maximize social welfare from its incumbent period onwards, whereby it takes as given the previous history of the economy as well as both the behavior of its later incarnations and of the private sector. The optimal policy problem therefore resembles a dynamic game between the private sector and all successive governments. The private sector acts as a Stackelberg follower, whereas the governments play Nash among each other and act as Stackelberg leaders against the private sector. For simplicity, and following the dominant approach in the macroeconomic literature, we restrict attention to stationary Markov-perfect equilibria of this policy game.

In a Markov-perfect equilibrium, strategies depend only on a minimal payoff-relevant state of the economy. For the present model with sticky prices this state is comprised of the variables b , m , a and g .⁵ The government today anticipates how future policies depend on current policy via the inherited state of the economy. Specifically, it perceives that, from the next period onwards, choices for v , π , w , q , m' , b' are governed by the rules \mathcal{V} , Π , \mathcal{W} , \mathcal{Q} , \mathcal{M} , and \mathcal{B} as in $v' = \mathcal{V}(b', m', a', g')$, $\pi' = \Pi(b', m', a', g')$, etc.

The optimization problem of the discretionary government is therefore given by:

$$\max_{v, \pi, w, q, b', m'} u(\hat{c}(\cdot)) - \alpha \hat{h}(\cdot) + \beta E \mathcal{U}(b', m', a', g') \quad (17)$$

subject to the constraints

$$\begin{aligned} 0 &= \hat{\tau}(\cdot) w \hat{h}(\cdot) + m' + qb' - g - \frac{m+b}{1+\pi}, \\ 0 &= \left(w - \frac{\theta-1}{\theta} a \right) \hat{h}(\cdot) \hat{\lambda}(\cdot) - \frac{\kappa}{\theta} \hat{\lambda}(\cdot) \pi (1+\pi) + \beta \frac{\kappa}{\theta} E \left\{ \hat{\lambda}'(\cdot) \Pi(\cdot) (1+\Pi(\cdot)) \right\}, \\ 0 &= \hat{\lambda}(\cdot) - \beta E \left\{ \frac{\hat{\lambda}'(\cdot) [1 + \mathcal{V}(\cdot)^2 s'(\mathcal{V}(\cdot))]}{(1+\Pi(\cdot))} \right\}, \\ 0 &= \hat{\lambda}(\cdot) q - \beta E \left\{ \frac{\hat{\lambda}'(\cdot)}{1+\Pi(\cdot)} \right\}. \end{aligned} \quad (18)$$

For better readability we have omitted the arguments of the functions \hat{c} , \hat{h} , $\hat{\tau}$, $\hat{\lambda}$, \mathcal{V} , and Π . Notice further that, because all future governments are perceived to employ the policy rules \mathcal{V} , Π , etc., the continuation value function $\mathcal{U}(b', m', a', g')$ is implicitly defined by the recursion

$$\mathcal{U}(b', m', a', g') = u(\hat{c}(\mathcal{V}(\cdot), \Pi(\cdot), m')) - \alpha \hat{h}(\mathcal{V}(\cdot), \Pi(\cdot), m', a', g') + \beta E \mathcal{U}(\mathcal{B}(\cdot), \mathcal{M}(\cdot), a'', g'').$$

⁵Here and in what follows we use recursive notation, i.e., we drop time indices and use primes to indicate next-period values.

In a stationary Markov-perfect equilibrium all governments employ the same policy rules. These rules must thus satisfy the following fixed-point property: If the current government anticipates all future governments to employ the rules $\{\mathcal{V}^*, \Pi^*, \mathcal{W}^*, \mathcal{Q}^*, \mathcal{M}^*, \mathcal{B}^*\}$, then the current government finds it optimal to follow the very same policy rules $\{\mathcal{V}^*, \Pi^*, \mathcal{W}^*, \mathcal{Q}^*, \mathcal{M}^*, \mathcal{B}^*\}$. Therefore, no government will find it worthwhile to deviate, and policies are time-consistent. Appendix A derives the first-order optimality conditions characterizing the stationary Markov-perfect equilibrium.

4 Numerical Solution and Calibration

For the model described in the previous section, the equilibrium policy functions cannot be computed in closed form. We thus resort to computational methods and derive numerical approximations to $\{\mathcal{V}^*, \Pi^*, \mathcal{W}^*, \mathcal{Q}^*, \mathcal{M}^*, \mathcal{B}^*\}$. Local approximation methods are not appropriate for this purpose because the model's steady state around which local dynamics should be approximated is endogenously determined as part of the model solution and thus a priori unknown. In light of this difficulty, we resort to a global solution method. Specifically, we employ the Galerkin projection method described in Judd (1992) and compute fourth-order accurate polynomial approximations to the equilibrium policy functions.⁶

Before solving the model numerically, functional forms must be specified and values must be assigned to structural parameters. Table 1 summarizes our choices. We set $\beta = 1/1.04$, which is a standard value for models with annual data. The utility function u is assumed to be of the CES type; the intertemporal elasticity of substitution is set to one half ($\sigma = 2$) which is in the middle of the parameter range typically considered in the literature. Moreover, a value of $\sigma > 1$ is essential for Markov-perfect policies to generate the empirically relevant scenario of a steady state with positive government debt, $b > 0$.⁷ The elasticity of substitution between intermediate goods is chosen as $\theta = 20$, which implies a monopolistic mark-up of approximately 5%, similar to Siu (2004). As for the price adjustment cost parameter κ , we will postulate different numerical values. In our benchmark calibration prices are flexible ($\kappa = 0$), but later on we consider values up to $\kappa = 2$. We choose to examine the interval $[0, 2]$ because in this range the effects of price stickiness are most relevant.⁸ A further motivation is that the value $\kappa = 2$ is equivalent to a Calvo parameter implying that on average firms re-optimize prices every six to seven months (cf. Keen and Wang, 2007), which is well in line with empirical

⁶Given that our model has four state variables, higher-order approximations are computationally infeasible. However, numerical accuracy checks show that the fourth-order approximation is sufficiently accurate for our purposes. Normalized errors in the model's Euler equations are well below 0.01% of consumption, such that the key simulation results can be considered immune to approximation error.

⁷For further details on this aspect, see Section 5.1 below.

⁸See Figures 1 and 3 in Schmitt-Grohe and Uribe (2004), as well as Figure 3 in this paper.

Table 1: Benchmark calibration: functional forms and parameter values

Description	Functional Form / Value
Period utility function	$u(c) = \frac{c^{1-\sigma}-1}{1-\sigma}$
Nominal rigidities (a la Rotemberg)	$\frac{\kappa}{2}\pi_t^2$
Transaction cost function	$s(v) = A_1v + A_2/v - 2\sqrt{A_1A_2}$
Discount factor	$\beta = 1/1.04$
Intertemporal elasticity of substitution	$1/\sigma = 0.5$
Marginal utility of leisure	$\alpha = 10.4$
Price elasticity of demand	$\theta = 20$
Size of price adjustment costs	$\kappa = 0$
Transaction costs	$A_1 = 0.137$
Transaction costs	$A_2 = 2.3$
Steady-state government expenditures	$\bar{g} = 0.06$
Persistence of government expenditures	$\rho_g = 0.8$
Expenditure innovation volatility	$\sigma_g = 0.04$
Persistence of technology process	$\rho_a = 0.82$
Technology innovation volatility	$\sigma_a = 0.023$

evidence (Bils and Klenow, 2004; Nakamura and Steinsson, 2008). The technology parameters are set to $\rho_a = 0.82$ and $\sigma_a = 0.023$, while the preference parameter α is selected such that labor supply in steady state is roughly equal to one third of the time endowment; this yields $\alpha = 10.4$. The government expenditure parameters are chosen in line with U.S. data for 1960-2006 available from Martin (2009). Government spending in steady state is set to $\bar{g} = 0.06$, corresponding to roughly 18% of output; $\rho_g = 0.8$, matching the autocorrelation coefficient of government expenditures in the data; and $\sigma_g = 0.04$ such that government spending differs by roughly four percentage points from its average. Finally, following Schmitt-Grohe and Uribe (2004), the transaction cost function is parameterized as $s(v) = A_1v + A_2/v - 2\sqrt{A_1A_2}$. Unlike these authors, however, we do not pin down the parameters A_1 and A_2 using money demand regressions but rather calibrate them.⁹ Our calibration of A_1 and A_2 ensures that the model generates a steady state velocity of $v^* = 4.3$, which is in line with the average velocity in the U.S. data for $M1$, and a ratio of government debt¹⁰ to GDP of approximately 30%; the resulting parameter values are $A_1 = 0.137$ and $A_2 = 2.3$.

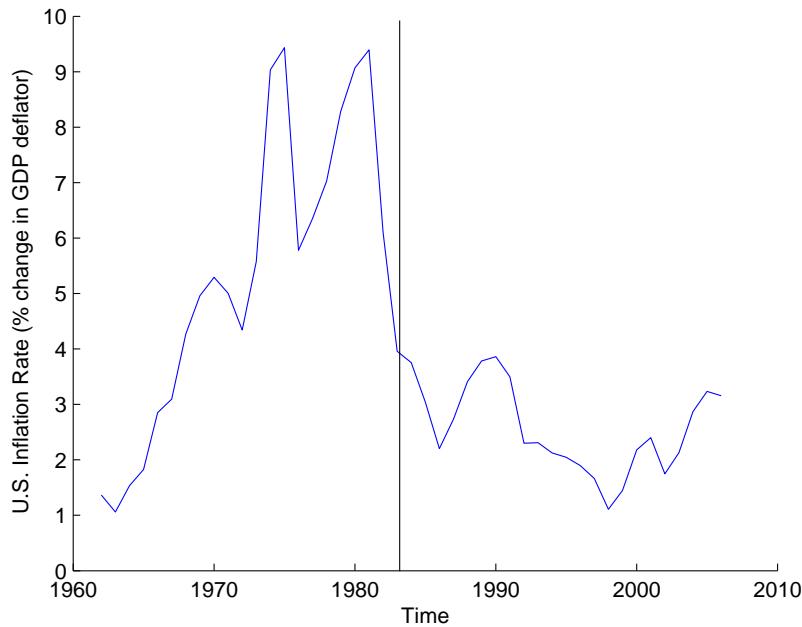
⁹We found that the transaction cost parameters are only weakly identified by money demand regressions. Specifically, the regression estimates for A_1 and A_2 have very large standard errors and are sensitive to the data sample employed (cf. Cooley and Hansen, 1991). In fairness to Schmitt-Grohe and Uribe (2004) let us emphasize, however, that their results are very robust to the numerical choices for A_1 and A_2 .

¹⁰Government debt in our model relates to the net asset position between the private and the public sector. Its empirical counterpart, therefore, is not gross federal debt, but government debt held by the public net of holdings by Federal Reserve Banks. This debt aggregate averaged at about 30% of GDP over 1960-2006, and has recently peaked at 47% of GDP in December 2009 (Council of Economic Advisers, 2010, p. 426).

5 Results

This section contains the main results of our analysis and confronts the model's predictions regarding inflation dynamics with the empirical evidence in the U.S. since the Volcker disinflation of the early 1980s.¹¹ As visualized in Figure 1, annual inflation rates in the U.S. averaged at roughly 4% over the time period 1962-2006 with a standard deviation of about 2% and a first-order autocorrelation coefficient around 0.8. Considering only the period after the Volcker disinflation, 1983-2006, inflation was on average around 2.6% with a standard deviation of 0.8% and an autocorrelation coefficient of slightly below 0.8.

Figure 1: The U.S. GDP deflator 1962-2006



Against this background, we first show that, irrespective of the degree of nominal rigidities, inflation rates under discretionary policies are positive on average and persistent. Hence, we demonstrate how our discretionary model improves upon Ramsey models of optimal fiscal and monetary policy in generating inflation dynamics in line with the empirical evidence. We also provide a detailed analysis of the mechanism underlying these dynamic properties. Finally, we turn to the dynamics of public debt under sticky prices and show that, in contrast to the Ramsey framework, debt does not display a near-random walk behavior.

¹¹The inflation dynamics experienced in the U.S. are similar to those in many other developed economies during this time.

Table 2: Dynamics

x	mean(x)	std(x)	corr(x', x)	corr(x, y)	corr(x, a)	corr(x, g)
$\kappa = 0$						
π	26.8860	4.1799	0.7822	0.0087	-0.3204	0.7577
R	31.9527	4.3741	0.9218	0.0425	-0.3395	0.8737
τ	15.2300	0.8307	0.7241	0.0712	-0.3526	0.9177
y	0.3293	0.0068	0.8109	1.0000	0.9071	0.4195
c	0.2684	0.0066	0.8284	0.7100	0.9374	-0.3371
b	0.1016	0.0025	0.7266	0.7090	0.7602	0.1194
$\kappa = 0.25$						
π	4.055	1.2699	0.6398	-0.2115	-0.5551	0.6595
R	8.6677	1.7586	0.8575	-0.4512	-0.7326	0.6213
τ	19.5394	1.2618	0.7922	0.1216	-0.3297	0.9338
y	0.3289	0.0067	0.8412	1.0000	0.8913	0.4372
c	0.2684	0.0064	0.8662	0.6925	0.9324	-0.3363
b	0.0980	0.0028	0.9068	0.0190	0.1030	0.4401
$\kappa = 0.5$						
π	2.5744	0.9648	0.7129	-0.1997	-0.5443	0.6171
R	6.6534	1.5874	0.8354	-0.4312	-0.7766	0.5456
τ	19.8609	1.2751	0.7851	0.1316	-0.3396	0.9247
y	0.3289	0.0066	0.8447	1.0000	0.8822	0.4525
c	0.2685	0.0063	0.8768	0.6900	0.9323	-0.3253
b	0.0919	0.0048	0.9691	-0.0280	-0.1167	0.4484
$\kappa = 1$						
π	1.1429	0.6677	0.7879	-0.1845	-0.4758	0.5243
R	5.1588	1.3653	0.7990	-0.5025	-0.8152	0.4578
τ	19.9525	1.2531	0.7782	0.1488	-0.3310	0.9181
y	0.3291	0.0066	0.8461	1.0000	0.8674	0.4735
c	0.2688	0.0061	0.8848	0.6878	0.9331	-0.3090
b	0.0762	0.0089	0.9889	-0.0578	-0.1670	0.3774
$\kappa = 2$						
π	0.4544	0.3878	0.8000	-0.1571	-0.4050	0.4757
R	4.0825	1.5796	0.7856	-0.4477	-0.7545	0.4840
τ	19.7160	1.3372	0.7816	0.1412	-0.3237	0.9109
y	0.3296	0.0066	0.8469	1.0000	0.8661	0.4682
c	0.2694	0.0061	0.8889	0.6876	0.9274	-0.3149
b	0.0504	0.0104	0.9932	-0.0628	-0.1311	0.3268

Note: The numbers reported are computed as averages over $N = 500$ simulations, each simulation of length $T = 1000$. The same realizations of the model's two exogenous shocks are used for each panel.

5.1 Optimal policy dynamics and inflation persistence

Table 2 presents simulation-based moments for the key variables in our model: inflation, the net nominal interest rate, labor taxes, output, consumption, and real debt. The values reported are computed as averages over 500 simulations of 1000 time periods each. Our central observation from Table 2 is that inflation rates are positive on average and persistent, and that these qualitative properties obtain independently of whether prices are flexible or sticky. By contrast,

the *quantitative* effects of price stickiness on inflation dynamics are not negligible; already a modest degree of rigidity has substantial effects: With $\kappa = 0.5$ average annual inflation is down to below 3%, compared to approximately 26% under flexible prices.¹² Indeed, for nominal rigidities in the range of $\kappa = 0.5$, the inflation dynamics are in line with the empirical evidence discussed above.¹³ At the same time, they contrast sharply with findings in the Ramsey literature (Schmitt-Grohe and Uribe, 2004) according to which optimal inflation typically ranges between zero and the (negative) value called for by the Friedman rule, and displays almost zero persistence.

The intuition behind this striking difference in optimal policy prescriptions is best understood as follows. First, a basic principle of optimal taxation explains why optimal inflation rates are positive: Once money demand is determined, the elasticity of consumption with respect to its effective price p/v is unitary; see (3). Conversely, anticipated changes in the effective price of consumption induce variations in money demand as determined by the intertemporal elasticity of substitution $1/\sigma$. Therefore, when $\sigma > 1$, future consumption is inelastic relative to current consumption. This gives the government a discretionary incentive to trade current distortions for future distortions, i.e., to increase current consumption at the expense of higher future indebtedness.¹⁴ In equilibrium, this *intertemporal elasticity effect* must be balanced by economic costs associated with increasing current consumption. As is evident from equation (3), an increase in consumption can either be accommodated via a decrease in the price level or an increase in velocity. Hence, costs from a discretionary increase in consumption arise if and only if both these channels are costly to exercise. For deflation to be costly, the amount of outstanding nominal debt must be positive such that lower prices raise the real value of the government's liabilities (Martin, 2009). For increases in velocity to be costly, v must be above the satiation level v . This effect drives monetary policy away from the Friedman rule, and we observe positive nominal interest rates in equilibrium. By the Fisher relationship, these translate into positive inflation rates.

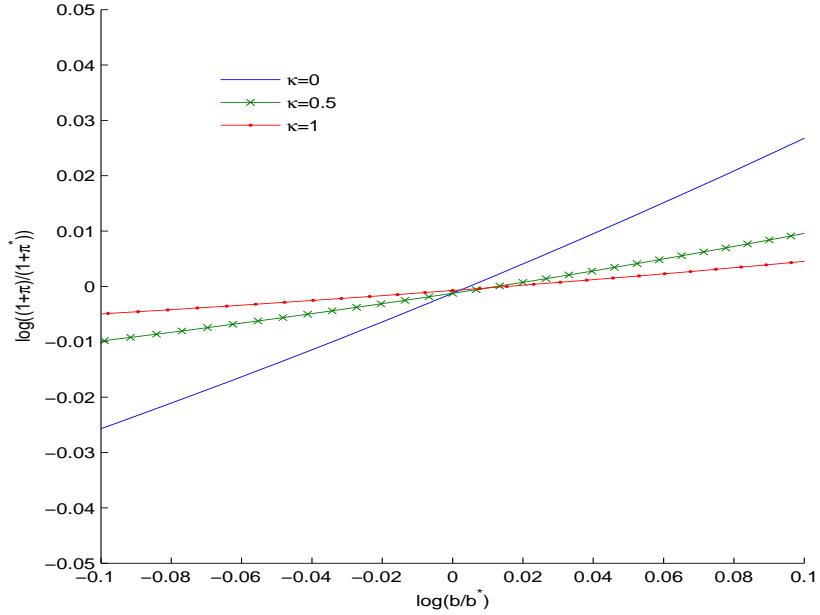
A similar argument explains why optimal inflation rates under discretion are persistent.

¹²We also assessed the robustness of our quantitative findings with respect to variations in the elasticity of demand. Smaller values of θ are associated with a substantial increase in the average level of inflation, while there is only a very modest rise in the autocorrelation. Appendix B details simulation-based moments for the case of flexible prices, comparing our baseline of $\theta = 20$ with the scenario of perfectly competitive product markets ($\theta = \infty$). The results reported there also make clear that, qualitatively, the inflation bias familiar from environments with monopolistic competition and sticky prices does not play an important role for our results. In particular, optimal inflation rates are positive (and persistent) even under perfect competition.

¹³Notice that by choosing a particular value of κ , one can effectively pin down the average inflation rate in the sticky price model. However, this has effects on the volatility and persistence of inflation. We believe that our model is in line with observed inflation dynamics because it simultaneously matches *all three* statistics (mean, standard deviation, autocorrelation coefficient).

¹⁴The argument is familiar from the cash-in-advance economies where velocity is exogenous and equal to one; see Diaz-Gimenez, Giovannetti, Marimon, and Teles (2008) and Martin (2009).

Figure 2: Inflation policy under flexible and sticky prices

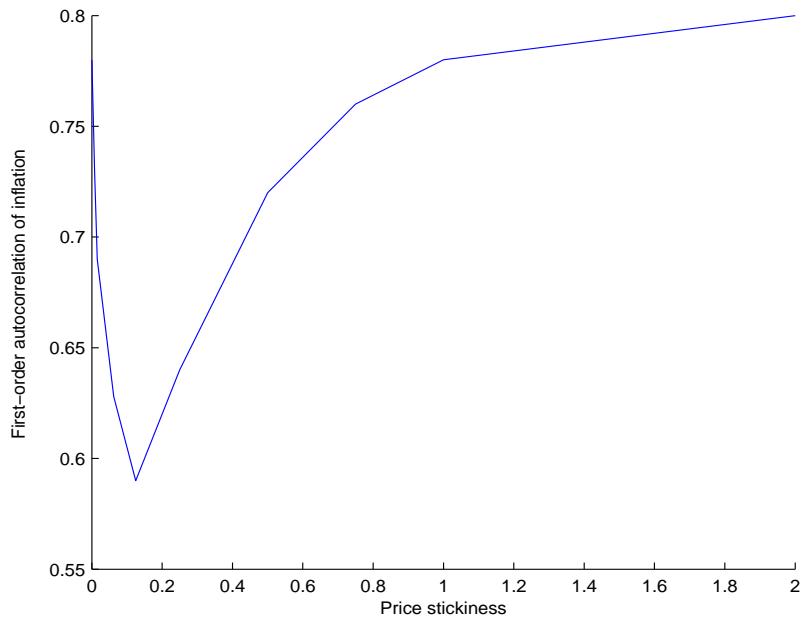


Note: On the horizontal axis we plot the percentage deviation of the debt-to-money ratio from its steady state level, and on the vertical axis the percentage deviation of inflation from its steady state level. The technology and government expenditure levels are fixed at the steady state levels $a = 1$ and $g = \bar{g}$, respectively.

Recall that, in an equilibrium with $\sigma > 1$, it is not sufficient that increases in velocity are costly, but decreases in the price level must be costly, too. Such costs arise because government debt trades in nominal terms, implying that the deflation needed to increase current consumption hurts the government because it increases the real value of its liabilities. Put differently, the government generally has an incentive to create inflation in order to monetize nominal debt. Since the magnitude of this *nominal debt effect* depends strongly on the amount of outstanding liabilities, realized inflation rates are increasing in the level of debt. This property is illustrated in Figure 2, which plots the equilibrium inflation policy as a function of the endogenous state variable b . On the other hand, the desire to smooth consumption in the face of stochastic shocks makes the government implement a relatively smooth path for debt. Therefore, real debt b is highly persistent, and due to the correlation between the two variables, the persistence in debt carries over to inflation.

Comparing the different panels of Table 2, we observe that the level of inflation decreases sharply in the price stickiness parameter κ . This reduction can be decomposed into two effects. The first and obvious effect is that, at all levels of government debt, the government chooses a

Figure 3: Inflation persistence and price stickiness



lower inflation tax in the face of the resource losses due to price adjustment costs. The second effect is via the reduced (average) level of debt, which further reduces the incentive to monetize nominal liabilities and therefore inflation. To understand why the level of debt decreases due to price adjustment costs, recall that, when prices are flexible, the discretionary government uses inflation as one of its main shock absorbers.¹⁵ The larger is the stock of debt, the better inflation can perform this role. Hence, besides its obvious negative effects on the government's budget constraint, a larger stock of debt can be helpful under flexible prices to stabilize the economy in response to shocks. However, this positive effect of the debt-stock is diminished under sticky prices since it becomes more costly to vary inflation in response to macroeconomic shocks. The policy-maker thus has an incentive to further reduce the stock of debt.

Finally, notice that while the level of inflation is clearly decreasing in the price stickiness parameter κ , the effect of κ on inflation persistence is non-monotonic. This latter property is emphasized in Figure 3, which plots the degree of inflation persistence (measured by the average first-order autocorrelation of the simulated inflation series) as a function of κ . At the flexible price benchmark inflation persistence sharply decreases in κ , but already at very low levels of κ it starts to increase. The intuition behind this property is best understood as follows. Recall that, in the model under consideration, the level of government debt is the

¹⁵Under flexible prices the volatility of inflation is at about 4.2%, while it is reduced to about 1.0% under sticky prices ($\kappa = 0.5$). Thus, as price stickiness increases, the task of macroeconomic stabilization is increasingly shifted towards taxes and variations in debt; compare Table 2.

principal determinant of inflation. Specifically, the government's inflation incentives and, thus, equilibrium inflation are increasing in debt. Under sticky prices, the convexity of the price adjustment costs implies that the reduction of the government's inflation incentive is stronger at high levels of debt (or inflation). This property reduces the correlation between inflation and the level of debt, as confirmed by the policy functions depicted in Figure 2. Consequently, for a given degree of persistence in debt this effect leads to a lower degree of inflation persistence. On the other hand, introducing sticky prices increases the persistence of debt since it limits the shock-absorbing role of inflation (Schmitt-Grohe and Uribe, 2004; Siu, 2004). This latter effect leads to a higher degree of inflation persistence. Whether inflation persistence increases or decreases due to price stickiness depends therefore on which of the two effects dominates.

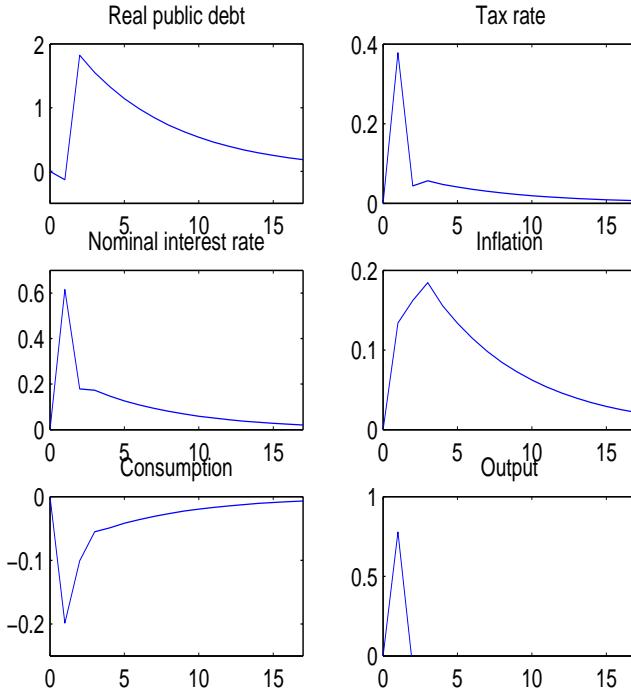
5.2 Mean-reverting debt dynamics

In the previous section we have argued that the persistence of debt increases considerably with the degree of price stickiness κ and that the underlying mechanism is familiar from the Ramsey literature. This raises the question of whether debt under discretionary policies also displays the *near-random walk property* familiar from this literature. In the following, we show that this is not the case.

To this end, we examine whether a temporary innovation to the public budget is financed by a permanent increase in (taxes and) debt. Figure 4 displays the impulse response to an uncorrelated government purchases shock for a sticky price model with adjustment cost parameter $\kappa = 1$. The pattern of adjustment shows that, in contrast to the Ramsey framework (Schmitt-Grohe and Uribe, 2004), both taxes and debt return to their pre-shock values. In other words, government debt is mean-reverting, consistent with the empirical behavior of U.S. public debt and deficits documented in Bohn (1998). The government responds to an expenditure shock in period one by simultaneously issuing public debt, raising the tax rate, and printing money.¹⁶ This policy reduces private consumption and stimulates economic activity such that the aggregate resource constraint is satisfied at the higher level of public expenditures. In period two, government expenditures return to their pre-shock level, but the government has a higher amount of debt outstanding which must be serviced in the following periods. As revealed by the impulse responses shown in Figure 4, the government essentially achieves this by means of higher taxes and a steady monetary expansion. Inflation peaks two years after the shock and then only gradually returns to its steady state level; several years after the shock has occurred inflation is still noticeably above its pre-shock level. On the other hand, the government in period two reduces the labor tax almost to the pre-shock level. This stimulates labor effort and

¹⁶Notice that nominal debt is initially inelastic such that the instantaneous rise in the price level reduces the real value of debt in period one.

Figure 4: Impulse responses to an i.i.d. government purchases shock



Note: The size of innovation in government purchases is one standard deviation. The shock takes place in period one. Public debt, consumption, and output are measured in percent deviations from their pre-shock values. The labor income tax rate, the nominal interest rate, and the inflation rate are measured in percentage points. Prices are sticky ($\kappa = 1$).

helps to maintain a smooth consumption path, a feature of optimal policy that is familiar from the Ramsey literature.

The key mechanism behind this adjustment pattern is the fact that, absent intertemporal commitment, an increase in public debt accentuates the government's time-inconsistency problem. The associated distortions – increased inflation expectations which are propagated via the model's Phillips curve relationship and increased nominal interest rates which act as opportunity costs of holding money – imply that debt variations in response to adverse shocks are costly. The policy-maker therefore feels compelled to keep debt in close vicinity of its steady state level to which it eventually returns. Hence, the near-random walk property of debt that characterizes optimal Ramsey policies is overturned.

6 Related Literature

In terms of its central research question, the present paper contributes to a large literature concerned with inflation persistence. Fuhrer and Moore (1995) show that in the New Keynesian model nominal rigidities in the wage or price setting mechanism generate persistence in the price level but fail to produce persistence in inflation. They suggest backward-looking wage contracting as a remedy to fix this implausible prediction. Similarly, Gali and Gertler (1999) and Steinsson (2003) postulate that a fraction of producers set their prices according to a rule of thumb, whereas Christiano, Eichenbaum, and Evans (2005) propose partial indexation to past inflation. On the other hand, a number of recent papers have identified persistent changes in monetary policy as potential driving forces behind persistent inflation rates. Cogley and Sbordone (2008) and Ireland (2007) consider shifts in the central bank's inflation target which translate into drifts in trend inflation and, thus, induce inflation persistence. Similarly, Erceg and Levin (2003) propose a model of incomplete information where inflation persistence is generated via the private sector's signal extraction problem in the face of uncertainty about the monetary policy rule. Common to these contributions is their emphasis on *exogenous* changes in the monetary policy regime. Our paper complements this recent literature by presenting a model where optimal macroeconomic policies are determined *endogenously*.

In terms of methodology, our paper contributes to a growing literature on time-consistent optimal policy. This literature formulates the policy problem as a game between successive governments and analyzes Markov-perfect equilibria of this game. Klein and Rios-Rull (2003) and Klein, Krusell, and Rios-Rull (2008) use this approach to examine optimal fiscal policies and government expenditures when the government lacks commitment power. Ortigueira (2006) studies optimal taxation, focussing on the implications of different degrees of the government's within-period commitment. Diaz-Gimenez, Giovannetti, Marimon, and Teles (2008) examine the implications of indexed versus nominal debt on optimal policies; they show that nominal government debt can be a burden on monetary policy because it accentuates the monetary authority's time-inconsistency problem. Martin (2009) provides a positive theory of public debt; considering a cash-credit economy, he argues that the costs and benefits of surprise inflation pin down the equilibrium level of public debt under discretionary policy-making.¹⁷ Finally, Adam and Billi (2008, 2010) and Niemann (2011) study strategic monetary-fiscal interactions from an optimal taxation perspective; their focus is on the desirability of monetary conservatism under lack of commitment.

¹⁷Martin (2009) also studies the dynamics of debt, taxes, and inflation in an extension of his basic model where government expenditures follow a stochastic two-state Markov process. In simulations for this economy, which is akin to the flexible-price version of our model, he uncovers that inflation rates are positive on average and display substantial persistence. But his analysis falls short of providing a detailed account of the mechanism generating these properties; moreover, the role of nominal rigidities in this context is not examined.

7 Conclusion

This paper has examined the dynamic properties of inflation in a model of optimal fiscal and monetary policy under discretion. In this model, there is a single benevolent government which can only use distortionary tax instruments, but can issue nominal state-noncontingent debt to shift distortions over time. Under lack of commitment and with nominal public debt, the government's problem is to optimally trade off the benefits and costs of inflation. On the one hand, unanticipated inflation in our model is attractive since it reduces the real value of outstanding liabilities. On the other hand, inflation is costly because it reduces current consumption possibilities by increasing transaction costs. This critical trade-off generates a rationale for fiscal and monetary policies which lead to positive and persistent inflation rates in equilibrium. The key mechanism behind this finding is that the government's desire to smooth consumption implies that public debt is issued in response to macroeconomic shocks. Optimal discretionary policies generate persistent debt; and this persistence carries over to inflation. Calibrating the model to U.S. data after the Volcker disinflation, we obtain empirically plausible inflation dynamics. Our analysis furthermore identifies a non-monotonic effect of nominal rigidities on inflation persistence and shows that government debt under discretion is mean-reverting and thus does *not* display the near-random walk property familiar from the Ramsey literature.

Acknowledgements

We thank the editor, Paul Klein, and an anonymous referee for their comments and suggestions which have substantially improved this paper. We also thank Sanjay Chugh, Wouter Den Haan, Christian Ghiglino, Ken Judd, Eric Leeper, John Lewis, Fernando Martin, Monika Merz, Salvador Ortigueira, Michael Reiter, Stefanie Schmitt-Grohé, Martin Uribe, and seminar audiences at various Universities and conferences for valuable comments and suggestions. Previous versions of this paper have been circulated under the titles *Optimal Fiscal and Monetary Policy Without Commitment* and *Inflation dynamics under optimal discretionary fiscal and monetary policies*. The views expressed in this paper are solely the responsibility of the authors and should not be interpreted as reflecting the views of the Oesterreichische Nationalbank.

References

- ADAM, K., AND R. M. BILLI (2008): "Monetary conservatism and fiscal policy," *Journal of Monetary Economics*, 55(8), 1376–1388.
- (2010): "Distortionary fiscal policy and monetary policy goals," Discussion paper.
- BILS, M., AND P. J. KLENOW (2004): "Some Evidence on the Importance of Sticky Prices," *Journal of Political Economy*, 112(5), 947–985.
- BOHN, H. (1998): "The Behavior Of U.S. Public Debt And Deficits," *The Quarterly Journal of Economics*, 113(3), 949–963.
- CHARI, V. V., L. J. CHRISTIANO, AND P. J. KEHOE (1991): "Optimal Fiscal and Monetary Policy: Some Recent Results," *Journal of Money, Credit and Banking*, 23(3), 519–39.
- CHRISTIANO, L., M. EICHENBAUM, AND C. EVANS (2005): "Nominal Rigidities and the Dynamic Effects of a Shock to Monetary Policy," *Journal of Political Economy*, 113(1), 1–45.
- CHUGH, S. K. (2007): "Optimal inflation persistence: Ramsey taxation with capital and habits," *Journal of Monetary Economics*, 54(6), 1809–1836.
- COGLEY, T., AND A. M. SBORDONE (2008): "Trend Inflation, Indexation, and Inflation Persistence in the New Keynesian Phillips Curve," *American Economic Review*, 98(5), 2101–26.
- COOLEY, T. F., AND G. D. HANSEN (1991): "The Welfare Costs of Moderate Inflations," *Journal of Money, Credit and Banking*, 23(3), 483–503.
- COUNCIL OF ECONOMIC ADVISERS (2010): *Economic Report of the President*. U.S. Government Printing Office.
- DIAZ-GIMENEZ, J., G. GIOVANNETTI, R. MARIMON, AND P. TELES (2008): "Nominal Debt as a Burden on Monetary Policy," *Review of Economic Dynamics*, 11(3), 493–514.
- ERCEG, C. J., AND A. T. LEVIN (2003): "Imperfect credibility and inflation persistence," *Journal of Monetary Economics*, 50(4), 915–944.
- FUHRER, J., AND G. MOORE (1995): "Inflation Persistence," *The Quarterly Journal of Economics*, 110(1), 127–59.

- GALI, J., AND M. GERTLER (1999): “Inflation dynamics: A structural econometric analysis,” *Journal of Monetary Economics*, 44(2), 195–222.
- IRELAND, P. N. (2007): “Changes in the Federal Reserve’s Inflation Target: Causes and Consequences,” *Journal of Money, Credit and Banking*, 39(8), 1851–1882.
- JUDD, K. L. (1992): “Projection methods for solving aggregate growth models,” *Journal of Economic Theory*, 58(2), 410–452.
- KEEN, B., AND Y. WANG (2007): “What is a realistic value for price adjustment costs in New Keynesian models?,” *Applied Economics Letters*, 14(11), 789–793.
- KHAN, A., R. G. KING, AND A. L. WOLMAN (2003): “Optimal Monetary Policy,” *Review of Economic Studies*, 70(4), 825–860.
- KLEIN, P., P. KRUSELL, AND J.-V. RIOS-RULL (2008): “Time-Consistent Public Policy,” *Review of Economic Studies*, 75(3), 789–808.
- KLEIN, P., AND J.-V. RIOS-RULL (2003): “Time-consistent optimal fiscal policy,” *International Economic Review*, 44(4), 1217–1245.
- MARTIN, F. (2009): “A Positive Theory of Government Debt,” *Review of Economic Dynamics*, 12(4), 608–631.
- NAKAMURA, E., AND J. STEINSSON (2008): “Five Facts about Prices: A Reevaluation of Menu Cost Models,” *The Quarterly Journal of Economics*, 123(4), 1415–1464.
- NIEMANN, S. (2011): “Dynamic Monetary-Fiscal Interactions and the Role of Monetary Conservatism,” *Journal of Monetary Economics*, 58(3), 234–247.
- ORTIGUEIRA, S. (2006): “Markov-Perfect Optimal Taxation,” *Review of Economic Dynamics*, 9(1), 153–178.
- ROTEMBERG, J. J. (1982): “Sticky Prices in the United States,” *Journal of Political Economy*, 90(6), 1187–1211.
- SCHMITT-GROHE, S., AND M. URIBE (2004): “Optimal fiscal and monetary policy under sticky prices,” *Journal of Economic Theory*, 114(2), 198–230.
- SCHMITT-GROHE, S., AND M. URIBE (2010): “The Optimal Rate of Inflation,” in *Handbook of Monetary Economics*, ed. by B. M. Friedman, and M. Woodford, vol. 3 of *Handbook of Monetary Economics*, chap. 13, pp. 653–722. Elsevier.

SIU, H. E. (2004): “Optimal fiscal and monetary policy with sticky prices,” *Journal of Monetary Economics*, 51(3), 575–607.

STEINSSON, J. (2003): “Optimal monetary policy in an economy with inflation persistence,” *Journal of Monetary Economics*, 50(7), 1425–1456.

SVENSSON, L. E. O. (1985): “Money and Asset Prices in a Cash-in-Advance Economy,” *Journal of Political Economy*, 93(5), 919–44.

Accepted manuscript

Appendix A

This Appendix details the government's optimality conditions that must be satisfied in a Markov-perfect equilibrium. The optimal policy problem under discretion reads

$$\max_{v, \pi, w, q, b', m'} \left\{ \frac{\hat{c}(v, \pi, m)^{1-\sigma} - 1}{1-\sigma} - \alpha \hat{h}(v, \pi, m, a, g) + \beta E \mathcal{U}(b', m', a', g') \right\}$$

subject to the implementability conditions

$$\begin{aligned} 0 &= \hat{\tau}(v, \pi, m, w) w \hat{h}(v, \pi, m, a, g) + m' + qb' - g - \frac{m+b}{1+\pi}, \\ 0 &= \left(w - \frac{\theta-1}{\theta} a \right) \hat{h}(v, \pi, m, a, g) \hat{\lambda}(v, \pi, m) - \frac{\kappa}{\theta} \hat{\lambda}(v, \pi, m) \pi (1+\pi) \\ &\quad + \beta \frac{\kappa}{\theta} E \left\{ \hat{\lambda}(\mathcal{V}(\cdot), \Pi(\cdot), m') \Pi(\cdot) (1 + \Pi(\cdot)) \right\}, \\ 0 &= \hat{\lambda}(v, \pi, m) - \beta E \left\{ \hat{\lambda}(\mathcal{V}(\cdot), \Pi(\cdot), m') \frac{1 + \mathcal{V}(\cdot)^2 s'(\mathcal{V}(\cdot))}{1 + \Pi(\cdot)} \right\}, \\ 0 &= \hat{\lambda}(v, \pi, m) q - \beta E \left\{ \hat{\lambda}(\mathcal{V}(\cdot), \Pi(\cdot), m') \frac{1}{1 + \Pi(\cdot)} \right\}. \end{aligned}$$

Given \mathcal{V} and Π , and accounting for the arguments in the functions $\hat{\tau}$, \hat{h} , and $\hat{\lambda}$ in the implementability constraints, we can write them as

$$\begin{aligned} 0 &= \Sigma(b, m, a, g, v, \pi, w, q, b', m'), \\ 0 &= \Omega(m, a, g, v, \pi, w, b', m'), \\ 0 &= \Psi(m, a, g, v, \pi, b', m'), \\ 0 &= \Phi(m, a, g, v, \pi, q, b', m'). \end{aligned}$$

Let us denote by η^1 , η^2 , η^3 and η^4 the multipliers on these constraints. The first-order conditions for the government's problem under discretion then read¹⁸:

$$0 = \hat{c}^{-\sigma} \hat{c}_v - \alpha \hat{h}_v + \eta^1 \Sigma_v + \eta^2 \Omega_v + \eta^3 \Psi_v + \eta^4 \Phi_v, \quad (19)$$

$$0 = \hat{c}^{-\sigma} \hat{c}_\pi - \alpha \hat{h}_\pi + \eta^1 \Sigma_\pi + \eta^2 \Omega_\pi + \eta^3 \Psi_\pi + \eta^4 \Phi_\pi, \quad (20)$$

$$0 = \eta^1 \Sigma_w + \eta^2 \Omega_w, \quad (21)$$

$$0 = \eta^1 \Sigma_q + \eta^4 \Phi_q, \quad (22)$$

$$0 = \beta E \left\{ \eta^1 (\Sigma_b)' + \eta^1 \Sigma_{b'} + \eta^2 \Omega_{b'} + \eta^3 \Psi_{b'} + \eta^4 \Phi_{b'} \right\}, \quad (23)$$

¹⁸The computation of the derivatives contained in the first-order conditions is tedious but straightforward.

$$0 = \beta E \left\{ (\hat{c}')^{-\sigma} \hat{c}'_{m'} - \alpha \hat{h}'_{m'} + \eta^1'(\Sigma_m)' + \eta^2'(\Omega_m)' + \eta^3'(\Psi_m)' + \eta^4'(\Phi_m)' \right\} \\ + \eta^1 \Sigma_{m'} + \eta^2 \Omega_{m'} + \eta^3 \Psi_{m'} + \eta^4 \Phi_{m'}. \quad (24)$$

Of particular interest are the two *generalized Euler equations* (23) and (24). Equation (23) characterizes the government's optimal choice of future public indebtedness b' . It equates the discounted, expected utility loss associated with a tighter budget constraint in the future to the current (direct and indirect) utility gain caused by a marginal relaxation of the current budget constraint and the other implementability constraints. Similarly, equation (24) characterizes the government's optimal choice of future real balances m' , accounting for the current and future welfare effects of a marginal monetary expansion.

Appendix B

Table 3 provides simulation-based moments for the case of flexible prices ($\kappa = 0$). The first panel considers perfectly competitive product markets and the second one our baseline calibration with monopolistic competition and mark-ups of 5.26%. A comparison of the two panels of

Table 3: Dynamics under flexible prices ($\kappa = 0$)

x	mean(x)	std(x)	corr(x', x)	corr(x, y)	corr(x, a)	corr(x, g)
Perfect competition ($\theta = \infty$)						
π	15.1443	3.5622	0.7655	-0.0105	-0.3101	0.7019
R	19.7405	3.7042	0.9434	0.0245	-0.3331	0.8298
τ	16.1550	0.7889	0.7382	0.0759	-0.3558	0.9184
v	4.2694	0.0323	0.9673	0.0120	-0.3058	0.7594
y	0.3380	0.0070	0.8106	1.0000	0.9040	0.4246
h	0.3380	0.0077	0.7978	-0.6668	-0.9212	0.3794
c	0.2776	0.0067	0.8298	0.7281	0.9470	-0.3073
b/p	0.1098	0.0032	0.8133	0.5820	0.5492	0.3138
b	1.6904	0.0628	0.9693	0.0089	-0.2474	0.7549
Imperfect competition ($\theta = 20$)						
π	26.8860	4.1799	0.7822	0.0087	-0.3204	0.7577
R	31.9527	4.3741	0.9218	0.0425	-0.3395	0.8737
τ	15.2300	0.8307	0.7241	0.0712	-0.3526	0.9177
v	4.3725	0.0377	0.9533	0.0342	-0.3173	0.8197
y	0.3293	0.0068	0.8109	1.0000	0.9071	0.4195
h	0.3293	0.0075	0.8000	-0.6758	-0.9230	0.3763
c	0.2684	0.0066	0.8284	0.7100	0.9374	-0.3371
b/p	0.1016	0.0025	0.7266	0.7090	0.7602	0.1194
b	1.6561	0.0477	0.9598	0.0244	-0.2571	0.8015

Note: The numbers reported are computed as averages over $N = 500$ simulations, each simulation of length $T = 1000$. The same realizations of the model's two exogenous shocks are used for each panel.

Table 3 reveals that, unlike in an environment of full commitment, imperfect competition has no qualitative effect on optimal policy under discretion. In particular, the Friedman rule is not optimal, and optimal inflation rates are positive on average, even when product markets are perfectly competitive. Moreover, optimal inflation rates display substantial persistence even under flexible prices.

Accepted manuscript